

Trading flexible electricity consumption in spot markets under demand response uncertainty

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Abstract

The ability to trade demand response profitably on competitive electricity markets is necessary to ensure its feasibility as a future power system resource. In this work we develop a novel trading strategy for aggregated demand response offering load curtailment on the day-ahead and continuous trade intraday markets, considering uncertainty in the achievable curtailment. Our analysis reveals that despite significant uncertainty at long horizons, it is more profitable to trade on both markets instead of solely the intraday market. The impact of resource uncertainty on revenue is found to be significant, though high forecast accuracy is deemed unnecessary due to the structure of trades on the intraday market.

Keywords: Demand Response, Trading Strategies, Electricity Markets, Uncertainty, Stochastic Optimisation

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Nomenclature

Indices:

t	Time index
k	Time index relative to start-up of DR event
e	Index of environmental uncertainty state
s	Index of structural uncertainty scenario
n	Index of load curtailment component
o	Index of trade offer on the intraday market

Parameters:

λ_t^{DA}	Day-ahead price
λ_t^D	Down regulation price
λ_t^U	Up regulation price
π_ω	Probability of scenario ω , combining probabilities of structural uncertainty scenario s and environmental uncertainty state e
$P_{k,s,n}^{DR,scenario}$	Available load curtailment in scenario s for structural uncertainty
A_e	Proportion of scheduled load curtailment that can be achieved in DR response state e
$P_n^{component}$	Component n of the available load curtailment products
D_n	Maximum duration for which load curtailment component n can be active
S	Offer to sell energy on the intraday market (Sell trade)
B	Offer to purchase energy on the intraday market (Buy trade)

$(\cdot)_{t,o}^P$	Trade price for intraday buy or sell trade
$(\cdot)_{t,o}^V$	Trade volume for intraday buy or sell trade

Variables:

$\Delta_{t,\omega}^+, \Delta_{t,\omega}^-$	Positive and negative deviations between scheduled and realised load curtailment
$P_t^{DR,S}$	Load curtailment scheduled on the day-ahead market
$P_t^{DA,R}$	Volume of day-ahead trade that is maintained during intraday trading
P_t^{DR}	Combined load curtailment scheduled on all markets
$\gamma_{t,n}$	Proportion of DR component n scheduled
$P_{t,\omega}^{DR,R}$	Load curtailment realised in scenario ω

Binary Variables:

$v_{t,o}$	Indicator that a buy trade has been accepted
$w_{t,o}$	Indicator that a sell trade has been accepted
$u_{t,n}$	Indicator that DR component n is active
SU_t^{DR}	Indicator of the start-up of a load curtailment event
SD_t^{DR}	Indicator of the shut-down of a load curtailment event

1. Introduction

1 Flexibility in power system operations is a key priority in the current en-
2 vironment of uncertain energy supply, greater reliance on stochastic power
3 generation, and constrained generation and transmission capacities. At a time
4 when power system flexibility is at a premium, demand response (DR) presents
5 a logical solution. Activating the flexibility of the demand side is said to bring
6 about such advantages as supporting higher penetrations of renewable gener-
7 ation (De Jonghe et al., 2012), alleviating network congestion (Sundstrom and
8 Binding, 2010), and increasing power system reliability (Kirby, 2008), among

9 others (Strbac, 2008).

10 The ability to profitably trade DR alongside conventional power system re-
11 sources on competitive electricity markets is a prerequisite for the success of
12 this novel resource. Under current market frameworks, deviations from stated
13 production or consumption profiles are penalised, to encourage trading be-
14 haviour that supports the stable operation of the power system. This places
15 stochastic resources, such as DR, at a disadvantage as penalties resulting from
16 their inherent uncertainty can have implications for their business case. In this
17 work we assess the revenue that can be generated through the trade of aggre-
18 gated DR resources on competitive spot markets, considering the uncertainty
19 of the resource and the consequent impact on expected revenue.

20 Optimal trading and scheduling of perfectly known DR has been addressed
21 in a number of works. Scheduling of DR alongside conventional power system
22 resources is considered by Zerrahn and Schill (2015) and O'Connell et al. (2015).
23 Participation of residential demand response in the day-ahead and balancing
24 markets is considered by Ali et al. (2015), while an optimal trading strategy
25 for flexible batch processes is developed by Mohsenian-Rad (2015). Consider-
26 ation of DR uncertainty in trading and scheduling strategies is less commonly
27 addressed, but is incorporated into the electric vehicle charging strategy de-
28 veloped by Gonzalez Vaya and Andersson (2015) and the scheduling of ag-
29 gregated thermostatically controlled loads described by Hao et al. (2015). The
30 nature of demand response uncertainty is described in (Mathieu et al., 2011),
31 and its impact is highlighted by Zhao et al. (2013) and Gao et al. (2015). The
32 work presented in this article differs from existing research by collectively con-
33 sidering the inherent uncertainty of the DR that can be delivered at real time,
34 the physical characteristics and constraints of the population of flexible loads
35 offering this service, and the necessity to develop trading strategies that are
36 suitable for existing market structures, rather than focussing solely on a single
37 aspect of the problem.

38 Given the limited research attention that has been dedicated to trading
39 strategies for uncertain DR, it is necessary to draw inspiration from the estab-

40 lished field of trading strategies for stochastic wind power generators. Analyt-
41 ical results for optimal bidding of wind generators in forward markets consid-
42 ering the penalty of imbalances at real-time are provided in (Dent et al., 2011).
43 Bidding strategies for both the day-ahead market and continuous trade intra-
44 day market are provided in (Skajaa et al., 2015), and (Rahimiyan et al., 2011)
45 provides an evaluation of a number of alternative offering strategies for wind
46 power producers. While both DR and wind power are stochastic power system
47 resources, they differ fundamentally in their delivery of power and associated
48 power system services. Wind power generators are primarily limited by the
49 instantaneously available power in the wind, whereas DR aggregators have
50 more flexibility to schedule load curtailment, but are limited in magnitude and
51 duration of DR events by the uncertain operating conditions of the individual
52 participating responsive loads. This fundamental difference offers the oppor-
53 tunity to learn from existing works while providing a novel contribution in the
54 area of trading uncertain demand response.

55 This work addresses the lack of research on the trading implications of DR
56 uncertainty by developing a full methodology for the trade of uncertain aggre-
57 gated DR on spot electricity markets. This work offers two novel contributions
58 to the state of the art. Firstly, an optimal trading strategy for uncertain DR on
59 a continuous trade intraday market is presented, considering that the DR re-
60 source offers a load curtailment product. Secondly, a full analysis is provided
61 of the impact of DR uncertainty on the revenue that a market agent can gener-
62 ate on both the day-ahead and intraday markets. This evaluation is informed
63 by a detailed model of the uncertainty sources in demand response, and a com-
64 prehensive set of sensitivity studies.

65 This paper is structured as follows. Section 2 provides a detailed descrip-
66 tion of the trading strategies developed for the day-ahead and intraday mar-
67 kets, and models for DR uncertainty and scheduling are presented. Section 3
68 describes the case study framework employed in this work. The key research
69 questions considered and results of this work are presented in Section 4, and
70 closing remarks are provided in Section 5.

71 2. Methodology

72 2.1. Participation of Demand Response in Wholesale Electricity Markets

73 2.1.1. Market Structure

74 In this work we consider that the market agent representing the demand
75 response resource operates within the Nordic Electricity Market. The Nordic
76 market is selected here as it shares a common structure with many European
77 markets, facilitating the extension of the trading strategies developed in this
78 work to many markets outside the Nordic region.

79 In the Nordic market, the market agent can offer load curtailment in either
80 the day-ahead market, Elspot, or the intraday market, Elbas (Nord Pool Spot,
81 2016). Real-time imbalances must be purchased from or sold to the transmis-
82 sion system operator (TSO) at the regulating power price.

83 Participants on the *Elspot* day-ahead market submit offers to the market
84 operator Nord Pool before gate closure at 12:00, for delivery of energy from
85 00:00 of the following day. Each market offer consists of a price and volume,
86 and covers an hour. This market is cleared through an auction process.

87 *Elbas* is the continuous trade intraday market. It is a bilateral market where
88 offers to buy and sell energy are matched on a continuous basis by the market
89 exchange. Each offer on this market consists of a price, energy volume and
90 delivery hour. Trading on this market continues until one hour prior to the
91 delivery hour.

92 The real-time deviation between traded and realised energy volumes must
93 be accounted for through the *regulating power market*. The TSO of each market
94 region within the Nordic market operates the local regulating power market,
95 sourcing generators to supply up- and down-regulation. Regulating power
96 prices are related to the day-ahead price, λ^{DA} , as in (1). Production balance
97 responsables (PBRs) with a positive imbalance will sell their excess energy at
98 the down-regulating price, λ^D , while a shortfall in energy is purchased at the
99 up-regulating price, λ^U .

$$\lambda^D \leq \lambda^{DA} \leq \lambda^U \quad (1)$$

100 In this work, the market agent representing demand response is considered a
101 PBR as the resource it offers is controllable load curtailment, which is analo-
102 gous to a power plant operator offering power supply.

103 2.1.2. Conventions and Assumptions

104 Trades on the intraday market are denoted *buy trades* or *sell trades*. Buy
105 trades are those posted by one market participant seeking to purchase energy
106 from another. The DR market agent can accept buy trades and fulfil them
107 through load curtailment. Sell trades are those offered by one market partici-
108 pant seeking to sell energy to another participant. Sell trades can be accepted
109 by the DR market agent to manage energy shortfalls that occur due to uncer-
110 tainty. In this work, the ability of the DR market agent to issue buy or sell
111 trades on the market is not considered. The market agent is limited to accept-
112 ing existing trades, as simulation of the acceptance rate of such trades by other
113 market participants is complex and beyond the scope of this work.

114 In this work the day-ahead and intraday trading strategies are treated as
115 separate problems. The problem of considering the possibility that a more prof-
116 itable trade will appear on the intraday market when determining the optimal
117 day-ahead trading strategy is substantially more complex than the model de-
118 veloped here. This is an open research question that we leave for future work.
119 Consequently, in the modelling framework employed in this work it can oc-
120 cur that trades that are accepted day-ahead may offer less revenue than a trade
121 that is subsequently offered on the intraday market. In such a case, the intraday
122 trade will be accepted if the cost of not meeting the day-ahead trade obligation
123 is less than the revenue that is available through the intraday trade. Consider
124 for example the case where a day-ahead trade of 10MWh has been accepted at
125 a market clearing price of €30/MWh for 10:00, and at 07:00 on the same day
126 an intraday trade is posted of (€50/MWh, 10MWh) for delivery at 10:00, the
127 up-regulation price for 10:00 is expected to be €40/MWh according to the fore-
128 cast available to the DR market agent (10MWh at €40/MWh). The day-ahead
129 revenue of €300 is guaranteed as this has been accepted by the market, but if

130 this day-ahead trade is not fulfilled, the DR agent is liable to pay an expected
 131 penalty of €400. The intraday trade offers a revenue of €500, resulting in total
 132 expected revenue for the DR agent of €400 if the intraday trade is accepted
 133 (€300 + €500 - €400). In such a case, the DR agent will chose to accept this in-
 134 traday trade and cover the resulting net imbalance with upward regulation in
 135 the balancing market. A similar situation can occur between intraday trades as
 136 they can be posted at any time. For example, if at 08:00 a further trade is posted
 137 for delivery at 10:00 of (€60/MWh, 10MWh), this trade will be accepted and
 138 the net imbalance will be covered through the purchase of regulating power.

139 In the trading strategies that are developed in this work the DR resource
 140 is restricted to offering load curtailment only. Many flexible loads are capable
 141 of both load curtailment and load shifting demand response. Load shifting
 142 consists of a reduction in power consumption at time t and a corresponding
 143 increase in power consumption at time $t \pm k$, whereas load curtailment is only
 144 the reduction component. The reduction in power consumption that occurs
 145 during load shifting can be greater than that during load curtailment, as the
 146 operating state of the flexible appliance can be allowed to deviate further from
 147 the typical operating state due to the guaranteed energy recovery. Thus, it
 148 is possible that the load reduction component of load shifting could generate
 149 greater revenue than load curtailment, however the need to purchase energy
 150 for the recovery component could eliminate this additional revenue. Further
 151 research is necessary to explore this issue.

152 2.2. Day Ahead Trading

153 As stated in (2), the day-ahead trading strategy maximises the expected rev-
 154 enue with respect to the available point forecasts of day-ahead price and imbal-
 155 ance prices, and scenarios of realisable load curtailment, considering that the
 156 DR market agent is a price-taker. The optimisation is subject to the constraints
 157 on load scheduling (4)-(7). The deviation between the scheduled load curtail-
 158 ment, $P_t^{DR,S}$, and that which is realised, $P_t^{DR,R}$, is denoted $\Delta_{t,\omega}$. It is a stochastic
 159 variable dependent on scenarios for outcomes in load curtailment, indexed by

160 ω , where the probability of each outcome is denoted π_ω . The deviation can
 161 be decomposed into positive, $\Delta_{t,\omega}^+$, and negative, $\Delta_{t,\omega}^-$, components. The pos-
 162 itive deviation (excess curtailment) is sold at the down-regulation price, λ_t^D
 163 and contributes to the expected revenue. A negative deviation (shortfall in
 164 load curtailment) is purchased at the up-regulation price, λ_t^U and is a net cost.
 165 The problem is formulated as below, where the decision variables \mathbf{P} are the
 166 scheduled curtailment at each time point t .

$$\max_{\mathbf{P}} \sum_t \left(P_t^{DR,S} \lambda_t^{DA} - \sum_\omega \pi_\omega \left(\Delta_{t,\omega}^- \lambda_t^U - \Delta_{t,\omega}^+ \lambda_t^D \right) \right) \quad (2a)$$

subject to:

$$P_{t,\omega}^{DR,R} = P_t^{DR,S} + \Delta_{t,\omega} \quad \forall t, \omega \quad (2b)$$

$$\Delta_{t,\omega} = \Delta_{t,\omega}^+ - \Delta_{t,\omega}^- \quad \forall t, \omega \quad (2c)$$

$$\Delta_{t,\omega}^+, \Delta_{t,\omega}^- \geq 0 \quad \forall t, \omega \quad (2d)$$

167

168 2.3. Intraday Trading

169 The intraday trading strategy is implemented in a rolling horizon optimisa-
 170 tion framework. On each optimisation step, the strategy considers the available
 171 sell trades, S , buy trades, B , and trade obligations from the day-ahead market
 172 over the current horizon $[t, t+h]$. The optimisation will choose to accept trades
 173 that result in the maximum expected revenue, subject to the forecast regulating
 174 prices. Trades on the first time interval t will be met through realised curtail-
 175 ment and the optimisation process will repeat for the interval $[t+1, t+h+1]$.

176 On each step, the trade list is updated to include newly issued trades and
 177 to remove trades that have been cancelled or accepted by other parties on the
 178 market. The optimisation algorithm considers all open trades as well as trades
 179 that have been previously accepted by the DR agent. This allows the DR agent
 180 to accept newly issued buy trades if they offer greater revenue than previously

181 accepted buy trades, given that the resulting net imbalance must be covered
182 through the purchase of sell trades or regulating power.

183 All trades on the intraday market are assumed to be all-or-nothing trades,
184 where the trade must be accepted completely or not at all. Trades on Elbas are
185 categorised as *all-or-nothing* or *fill*, where fill trades can be accepted in part. The
186 trade type is not indicated on the data available for this study, thus differentia-
187 tion between trade types is not considered in the model.

188 The value of reserving DR resources for possible intraday trades that are
189 not visible in the current horizon, but which may be posted at a later time, is
190 not considered in this model.

191 To facilitate a fair assessment of the revenue generated through the trade
192 of DR, and the impact of its uncertainty, speculation is not permitted in the
193 trading strategy that is detailed here. To prevent speculation, the restriction is
194 imposed that it must be possible to meet all accepted buy trades through load
195 curtailment, subject to the constraints outlined in Section 2.5.

196 The mathematical formulation of the intraday trading strategy is detailed
197 in (3), and is subject to the DR scheduling constraints (4) - (7). The objective
198 function maximises the expected revenue, which is comprised of income from
199 buy trades that are accepted and the expected income from the sale of energy
200 on the regulating power market, minus expenditure from sell trades that are
201 accepted and the purchase of energy on the regulating power market. Trade
202 volumes and prices are denoted $(\cdot)_{t,o}^V$ and $(\cdot)_{t,o}^P$ respectively, where o is the
203 index of the trade, or offer. The binary variables $v_{t,o}$ and $w_{t,o}$ become non-zero
204 to indicate that a buy or sell trade has been accepted, respectively.

Speculation is prevented by (3b) and (3c). Equation (3b) states that the sum
of the buy trades accepted at time t and the portion of the day ahead trade
that is realised, $P_t^{DA,R}$, must not exceed the curtailment that can be provided
by the DR resource, P_t^{DR} . The optimisation can chose to realise a portion or
all of the day-ahead trading obligations, $P_t^{DR,S}$ as determined in (2), through
curtailment, as given in (3c). Speculation through the purchase of sell trades
is prevented by further constraints, though they are omitted here for brevity.

The net imbalance, defined in (3d), is the difference between the trading obligations from the day-ahead market plus the net intraday trade and the realised load curtailment. The net intraday trading position is comprised of trades that were accepted on previous optimisation steps, i , for trading during the current trading horizon plus trades that were newly accepted on this optimisation step. The imbalance is divided into positive and negative components, each of which is charged at the relevant regulating power price, as on the day-ahead market.

$$\max \sum_t \left(\sum_o \left(v_{t,o} B_{t,o}^V B_{t,o}^P - w_{t,o} S_{t,o}^V S_{t,o}^P \right) + \sum_\omega \pi_\omega \left(\Delta_{t,\omega}^- \lambda_t^U - \Delta_{t,\omega}^+ \lambda_t^D \right) \right) \quad (3a)$$

subject to:

$$\sum_o v_{t,o} B_{t,o}^V + P_t^{DA,R} \leq P_t^{DR} \quad \forall t \quad (3b)$$

$$P_t^{DA,R} \leq P_t^{DR,S} \quad \forall t \quad (3c)$$

$$\Delta_{t,\omega} = P_t^{DA} + \sum_o B_{t,o}^V (v_{t,o} (1 - v_{i-1,t,o}) + v_{i-1,t,o}) - \sum_o S_{t,o}^V (w_{t,o} (1 - w_{i-1,t,o}) + w_{i-1,t,o}) - P_{t,\omega}^{DR,R} \quad \forall t, \omega \quad (3d)$$

$$\Delta_{t,\omega} = \Delta_{t,\omega}^+ - \Delta_{t,\omega}^- \quad \forall t, \omega \quad (3e)$$

$$\Delta_{t,\omega}^+, \Delta_{t,\omega}^- \geq 0 \quad \forall t, \omega \quad (3f)$$

205

206 2.4. Modelling Uncertainty in Demand Response

207 Load curtailment is subject to a number of sources of uncertainty, which can
 208 be divided into the categories of *structural* and *environmental*. Structural uncer-
 209 tainty arises when the model used to describe the population of flexible loads
 210 and their flexibility is inaccurate. Environmental uncertainty arises when ex-
 211 ternal conditions such as ambient temperature, or interaction with end-users,
 212 induce variability into the realised response. Analysis of variability in load

213 curtailment events is provided by Mathieu et al. (2011).

214 The sources of uncertainty are dependent on the end-use considered for the
215 provision of demand response. In this work we employ the example resource
216 of supermarket refrigeration. The choice of this flexible end-use is due in part
217 to its suitability for the provision of demand response, and in part due to the
218 availability of data describing its demand response characteristics (O’Connell
219 et al., 2014).

220 *2.4.1. Structural uncertainty modelling*

221 The structural uncertainty is estimated by employing the time-series model
222 of a supermarket refrigeration described by O’Connell et al. (2014). Monte
223 Carlo simulations of the modelled system were employed to generate scenarios
224 of the possible response for a given curtailment event. The model employed
225 does not consider external stimuli such as ambient temperature, and assumes
226 that the supermarket employs model predictive control, such that deviations
227 from the prescribed power reference can be corrected on each control iteration.
228 Thus, the resulting scenarios only consider the model uncertainty and describe
229 the response that can be expected under ideal external conditions.

230 *2.4.2. Environmental uncertainty modelling*

231 Environmental uncertainty in supermarket refrigeration demand response
232 can be considered to come from two main sources: outdoor temperature, and
233 interactions with customers and store employees. In this work we focus on the
234 uncertainty resulting from human interaction, as this is expected by the authors
235 to have a greater impact on the certainty of the demand response that can be
236 provided. Furthermore, there is currently insufficient data to support a char-
237 acterisation of the impact of outdoor temperature on the certainty with which
238 demand response can be achieved in an operational sense. However, work
239 conducted by Rasmussen et al. (2015) has demonstrated how the relationship
240 between power consumption of a supermarket and weather conditions can be
241 modelled using transfer functions coupled with spline functions, which is a

242 promising indication that the work presented in this article can be adapted to
243 incorporate the relationship between demand response and outdoor tempera-
244 ture once supporting data becomes available.

245 In a supermarket it can be expected that there is significant disturbance to
246 the refrigeration system during periods in which there are many customers in
247 the supermarket, or when restocking of goods occurs. During the low activ-
248 ity night hours it can be expected that the available load curtailment is known
249 with more certainty. This time varying uncertainty can be represented by as-
250 suming that the system can occupy a number of states, and that the probability
251 of occupying each state is time varying. Each state represents the degree to
252 which the scheduled load curtailment can be achieved. This structure resem-
253 bles that of an inhomogenous Markov process (Madsen et al., 1985). In this
254 work, the probability of occupying a given state is defined for each hour of the
255 day, assuming that variations in uncertainty occur on a diurnal cycle.

256 The authors highlight that this characterisation of environmental uncer-
257 tainty is not founded on operational data of supermarkets participating in DR
258 programs, as there is currently no available data that would support the iden-
259 tification of this uncertainty distribution. In the absence of an appropriate data
260 source, it is necessary to approximate the distribution with an educated esti-
261 mate. Consequently, the numerical results presented in this work are intended
262 solely to provide an indication of the impact of uncertainty on the revenue that
263 can be generated, not a definitive analysis. Sensitivity studies are conducted to
264 assess the impact of the uncertainty distribution on the revenue outcome, and
265 to emphasize the need to dedicate further research to the identification of rep-
266 resentative uncertainty distributions to inform more comprehensive analysis.

267 *2.5. Scheduling Demand Response*

268 DR is subject to the same scheduling constraints in both of the energy mar-
269 kets considered. Here we consider that the DR agent can offer a number of
270 different curtailment products. Products are differentiated according to mag-
271 nitude and duration. Figure 1 illustrates a sample case where three products,

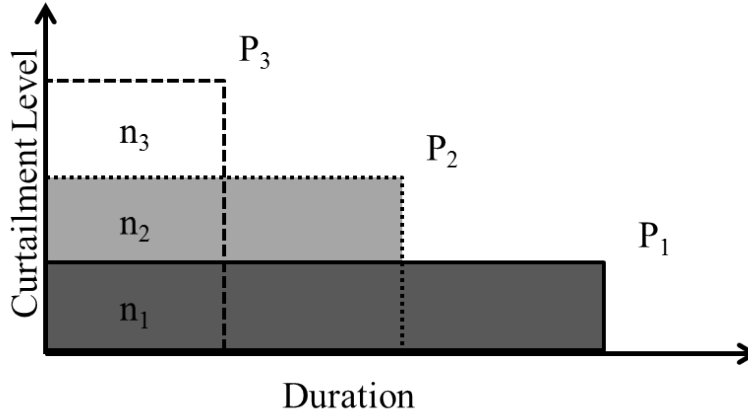


Figure 1: DR offer structure

272 P , can be offered to an energy market. In the mathematical formulation that
 273 follows, the offered products are defined in a stacked manner. For example,
 274 the magnitude of product P_2 is the summed magnitudes of components n_1 and
 275 n_2 , while the maximum duration of the product is limited to the duration of
 276 component n_2 , the highest active product component. Formulating the prob-
 277 lem in this manner alleviates the computational burden associated with the use
 278 of binary variables to differentiate between load curtailment products.

279 2.5.1. Component based products

The magnitude of each product component is denoted $P_n^{component}$. Load cur-
 tailment, P_t^{DR} can be scheduled up to the maximum allowable curtailment for
 a given product, as defined by the sum of its components. This is imposed in
 (4a). The binary variable $u_{t,n}$ indicates whether a given product component is
 active. Restrictions are placed on the value of $u_{t,n}$ to ensure that the compo-
 nents are activated sequentially, (4b). The start and end of a load curtailment
 event are denoted SU_t^{DR} and SD_t^{DR} respectively. These binary variables are
 activated by a change in the value of $u_{t,n}$. The behaviour of the start-up and

shut-down indicators is governed by (4c) - (4f).

$$P_t^{DR} \leq \sum_n u_{t,n} P_n^{component} \quad \forall t \quad (4a)$$

$$u_{t,n} \leq u_{t,n-1} \quad \forall t, n \quad (4b)$$

$$u_{t,n} - u_{t-1,n} = SU_{t,n} - SD_{t,n} \quad \forall t, n \quad (4c)$$

$$SU_t^{DR} \geq SU_{t,n} \quad \forall t, n \quad (4d)$$

$$SD_t^{DR} \geq SD_{t,n} \quad \forall t, n \quad (4e)$$

$$SU_t^{DR} + SD_t^{DR} \leq 1 \quad \forall t \quad (4f)$$

280

281 2.5.2. *Limited product duration*

The scheduled duration of a curtailment event is limited to the duration of the highest active product component, D_n . This is enforced in (5a) which states that the sum of active components over the duration of the DR event must be less than the duration of the highest active product component (multiplied by the number of components in the scheduled product, $\sum_{v=1}^n 1$). If a component n is not active, the expression $(1 - u_{t,n})$ becomes 1, causing the constraint to be non-binding. Consider for example the product P_2 illustrated in Fig. 1, the maximum sum of online indicators for components n_1 and n_2 over the duration of the product, two intervals, is four. This constraint assumes that $D_n < D_{n+1}$. Following a curtailment event, (5b) prevents the activation of any product component for a rest period, R . The end of a curtailment event is indicated by a change in online status for any product component n from 1 to 0. Consequently, the behaviour illustrated in the last element of Fig. 2 is prohibited by (5b), as n_2 ceases activity, which prevents activity in n_1 .

$$\sum_{\tau=t}^{t+D_n} \sum_{v=1}^n u_{\tau,v} \leq (D_n + (1 - u_{t,n})) \sum_{v=1}^n 1 \quad \forall t, n \quad (5a)$$

$$\sum_{\tau=t}^{t+R-1} (1 - u_{\tau,n}) \geq SD_t^{DR} R \quad \forall t, n \quad (5b)$$

282

283 *2.5.3. Permitted Scheduling*

To ensure that curtailment products with larger magnitudes are not scheduled for the longer duration of smaller magnitude products, it is necessary to ensure that product components cannot activate at arbitrary points, as imposed by (6a). The only time at which product components are permitted to activate is when an event start-up occurs, and only those product components that are activated at the start up time are permitted to be online for the duration of the product. The behaviour that this constraint prohibits is illustrated by the second element in Fig. 2. If the curtailment event concludes before the stated duration, the constraint becomes non-binding, allowing for the subsequent scheduling of other products. This is illustrated in the last two elements of Fig. 2, though of course the last element is prohibited. Furthermore, if a start up did not occur at the considered starting time t the constraint is not binding.

$$u_{\tau,n} \leq u_{t,n} + (1 - SU_t^{DR}) + \sum_{\tau'=t}^{\tau} SD_{\tau'}^{DR} \quad \forall \tau \geq t, \tau < t + D_n \quad (6a)$$

284

285 *2.5.4. Realised Uncertainty*

286 Uncertainty in the realised curtailment is considered in (7a) and (7b). Through
 287 the combination of these two constraints it is imposed that the realised load
 288 curtailment, $P_{t+k,\ell,s'}^{DR,R}$ is equal to the scenarios of realised curtailment $P_{k,s,n}^{DR,scenario}$
 289 (representing structural uncertainty) multiplied by a stochastic parameter of
 290 response availability A_e (representing environmental uncertainty). The stochastic
 291 indices s and e denote the uncertainty sets for structural and environmental
 292 uncertainty respectively, these were previously combined in the uncertainty
 293 index ω for simplicity. These constraints are non-binding if an event did not
 294 start at time t , or if the component corresponding to the load curtailment sce-
 295 nario is not active, $u_{t+k,n}$, or if a higher product component is active, $u_{t+k,n+1}$.

296 This is achieved through the M value, which is a large number that causes (7a)
 297 and (7b) to be non-binding under any of the above conditions. In this man-
 298 ner, each curtailment event is restricted by constraints concerning the highest
 299 active product component only.

As it is possible to schedule load curtailment at a level less than the maxi-
 mum allowable magnitude of a given product, it is necessary to scale the sce-
 narios accordingly. This is achieved by the scaling parameter $\gamma_{t,n}$ which com-
 pares the scheduled load curtailment P_t^{DR} to that defined by the product com-
 ponents. This scaling is essentially linear interpolation between the defined
 products, as it is not possible to define scenarios for the realised curtailment
 at every possible level of scheduled curtailment. To minimise the error intro-
 duced by this interpolation, curtailment products should be defined at regular
 intervals of curtailment magnitude. Each additional curtailment product in-
 troduces a further binary variable, increasing the computational complexity of
 the problem. Thus, a compromise must be found between the computational
 burden and accuracy required by the scheduling algorithm.

$$P_{t+k,e,s}^{DR,R} \geq P_{k,s,n}^{DR,scenario} A_e \gamma_{t+k,n} - \\ ((1 - SU_t^{DR}) + (1 - u_{t+k,n}) + u_{t+k,n+1})M \quad \forall t, n \quad (7a)$$

$$P_{t+k,e,s}^{DR,R} \leq P_{k,s,n}^{DR,scenario} A_e \gamma_{t+k,n} + \\ ((1 - SU_t^{DR}) + (1 - u_{t+k,n}) + u_{t+k,n+1})M \quad \forall t, n \quad (7b)$$

$$\gamma_{t,n} = \frac{\sum_{v=1}^n P_v^{component} - P_t^{DR}}{\sum_{v=1}^n P_v^{component}} \quad \forall t, n \quad (7c)$$

300

301 3. Case Study

302 This section describes the parameters of the case studies employed in this
 303 work.

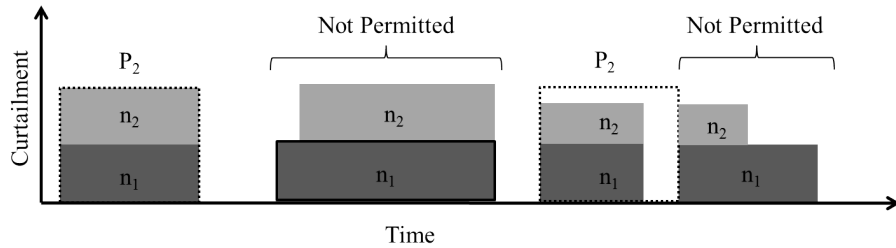


Figure 2: Illustration of permitted and prohibited scheduling

304 *3.1. Data Description*

305 Simulations conducted in this work consider historical price data at hourly
 306 resolution from each of the markets considered. The scheduling optimisations
 307 consider the most recently available point forecast of the relevant prices, while
 308 actual revenue is calculated using the realised prices. In order to achieve an
 309 overall representation of the performance of the trading strategy, simulations
 310 are conducted using data from four weeks in 2012; 23rd-29th April, 18th-24th
 311 June, 17th-23rd September, and 17th-23rd December.

312 The historical prices employed are point forecasts of the day-ahead and
 313 regulating power prices in the eastern Denmark pricing region, as available at
 314 the time of scheduling; realised prices on the day-ahead and regulating power
 315 market; and intraday trade offers, including information on when the offer
 316 was posted and when it was removed from the list of open trades. Price fore-
 317 casts for up- and down-regulation prices are issued hourly; trading on the day-
 318 ahead market considers the forecasts issued at 11:00 a.m. on the day before en-
 319 ergy delivery, whereas intraday trading considers the most up-to-date version
 320 of the forecast at the relevant hour. Forecasts of the up- and down-regulation
 321 prices are calculated from conditional probabilities of the deviation between
 322 the regulation and day-ahead price, a thorough description of the models em-
 323 ployed to derive the conditional probabilities can be found in Section III of
 324 (Skajaa et al., 2015), and (ENFOR, 2013).

325 *3.2. Simulation Framework*

326 The DR resource considered in the simulations that follow consists of 3000
327 supermarkets offering a maximum load curtailment of 10kW each. The popu-
328 lation of supermarkets is considered to offer three DR products: 30 MW cur-
329 tailment for one hour, 18 MW curtailment for up to two hours, or 15 MW cur-
330 tailment for up to three hours. These quantities are selected to ensure that the
331 temperature change that occurs on the refrigeration system during curtailment
332 events does not necessitate an energy recovery subsequent to the curtailment.
333 This is informed by studies from O'Connell et al. (2014).

334 Structural demand response uncertainty is represented through three sce-
335 narios for each of the demand response products offered.

336 Environmental demand response uncertainty for participation on the in-
337 traday market is represented in the form of six probability distributions for the
338 proportion of the requested demand response that is realised at a given time, as
339 are illustrated in Fig. 3. It is considered that the demand response resource can
340 occupy three possible states; fully responsive, 50% responsive, and not respon-
341 sive. Three of the probability distributions are time varying, while the second
342 set of three distributions are their time invariant counterparts, where the state
343 probabilities are the time averaged probability values from the first three dis-
344 tributions. The time varying probability distributions are designed such that
345 they represent situations in which there is a mild, moderate and extreme vari-
346 ation in state probabilities over the course of a day. It is assumed that there is
347 no variation in these distributions from one day to the next.

348 The intraday trading strategy is subject to an optimisation horizon of 7
349 hours. This value represents a compromise between a very short horizon which
350 would induce terminal effects, and a long horizon which is subject to signifi-
351 cant price forecast uncertainty. The selected horizon results from analyses of
352 the impact of horizon extent on revenue outcomes.

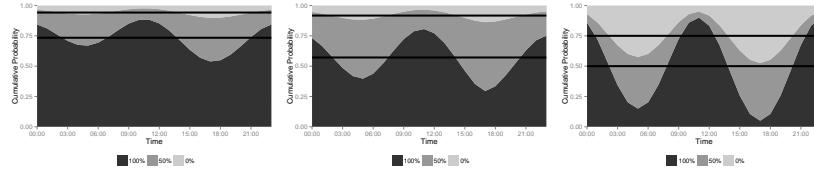
353 3.3. Assumptions

354 In the analyses that follow, all possible effort has been made to ensure re-
355 alistic results. However, in order to extract meaningful results it is necessary
356 to limit the scope of the studies and to make a number of simplifying assump-
357 tions.

358 Firstly, the demand response agent is limited to accepting existing intraday
359 trades, it may not issue trades of its own. This assumption restricts the revenue
360 that the agent can accrue. Limited liquidity on this market means that there
361 may be times at which the agent is capable of providing demand response but
362 there are no suitable open trades. Allowing the agent to post its own trades
363 might result in additional revenue, however it is not possible to realistically
364 simulate whether or not these trades are accepted by other market participants
365 within the scope of this work.

366 Secondly, all trades on the intraday market are assumed to be all-or-nothing
367 trades, where the trade must be fulfilled completely or not at all. Trades on
368 Elbas are categorised as all-or-nothing or fill, where fill trades can be accepted
369 in part. The dataset of Elbas trades employed in this work does not indicate the
370 trade type, necessitating this assumption. This assumption reduces revenue
371 as certain trades are excluded from consideration as they cannot be fulfilled
372 entirely.

373 Finally, it is assumed for simulation purposes that trade offers on the intra-
374 day market are assessed once an hour. In reality, offers are posted and accepted
375 at arbitrary times for energy delivery at set hours. To reflect this behaviour, it is
376 necessary to run the rolling horizon intraday trading optimisation every time
377 a new offer is posted. This level of detail is not warranted for a simulation
378 study, so it is assumed that all offers which are posted during a given hour are
379 evaluated together at the start of the following hour, regardless of the order
380 in which they were posted. It is not clear whether this assumption increases
381 or decreases the market revenue made by the demand response agent, as it
382 produces two conflicting effects: on one hand, the simultaneous assessment of
383 all trades posted in a given hour increases the revenue compared to assessing



(a) Base Distribution (b) Moderate Distribu- (c) Extreme Distribution
tion

Figure 3: Environmental uncertainty distributions considered in the case studies. The cumulative probabilities of the response states are indicated by the curved area plots (time varying distributions) and the horizontal lines (time invariant distributions).

384 each trade in turn as it is posted on the market, because the decision maker
 385 has full knowledge of all the available trades; on the other hand, by waiting
 386 to consider the acceptance of a given trade until the designated assessment
 387 time revenue is reduced, as advantageous trades may be missed because other
 388 market participants have accepted them.

389 4. Results and Discussion

390 In this section we present the results of simulations conducted to answer
 391 three key research questions.

392 4.1. Is participation on the day-ahead market profitable?

393 In this section the value of trading highly uncertain demand response at
 394 longer horizons in the day-ahead market is addressed, considering that trade
 395 can also occur at shorter horizons on the intraday market at greater certainty.
 396 The revenue generated through participation on the day-ahead and intraday
 397 markets is illustrated in Fig. 4. The combined revenue from the day-ahead
 398 and intraday markets is shown for a range of day-ahead demand response
 399 forecast accuracy levels for environmental uncertainty. This is compared to
 400 the case where no trading occurs on the day-ahead market. The *poor* fore-
 401 casts case considers that each of the achievable demand response states, 100%,
 402 50% and 0% are equiprobable, while the *moderate* forecast assumes that the

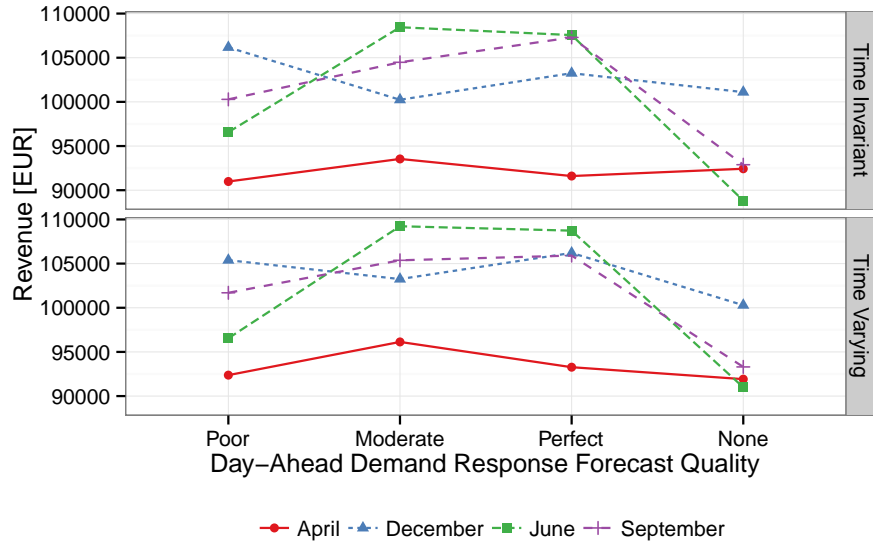


Figure 4: Expected revenue from trading on the day-ahead and intraday markets with a range of day-ahead DR forecast qualities.

403 DR resource is perfect (100% response at all times). The poor forecast there-
 404 fore under-estimates the response while the moderate forecast over-estimates
 405 it. The *perfect* forecast considers that the day-ahead optimisation employs the
 406 same uncertainty distribution of achievable load curtailment as the intraday
 407 trading optimisation. The demand response uncertainty distributions consid-
 408 ered for the intraday trading optimisation in this case are the time varying and
 409 time-invariant distributions from Fig. 3(a).

410 It can be seen in most of the studied cases that trading on the day-ahead
 411 market is advantageous, even when the DR forecast is poor. In many cases it
 412 can be seen that a moderate demand response forecast out-performs the per-
 413 fect forecast. This is because this forecast overestimates the demand response
 414 resource and offers more energy on the day-ahead market than can be deliv-
 415 ered. In doing so, the higher prices on the day-ahead market can be leveraged,
 416 and the imbalance that occurs at real-time can be corrected through either pur-
 417 chasing trades on the intraday market or on the regulating power market. This

418 strategy of overestimating the demand response resource on the day-ahead
419 market does not always result in higher revenue than a perfect forecast. If ad-
420 vantageously priced sell trades are not available on the intraday market, the
421 energy shortfall must be purchased at the regulating power price, which is
422 at least as high as the day-ahead price. A comprehensive year-long study is
423 required to determine if this trend of higher day-ahead prices prevails over a
424 longer period. As the current study is intended solely to highlight the complex-
425 ity of trading uncertain demand response, this further analysis will be consid-
426 ered for future work.

427 It should be noted here that the expected revenue range is approximately
428 €90,000-€110,000. As the DR resource consists of 3000 supermarket providing
429 curtailment, this amounts to a revenue of approximately €30-37/week per par-
430 ticipating supermarket. This is a very small sum, which is unlikely to justify
431 the investment necessary to provide DR. This does not however rule out the
432 possibility of profitable participation in spot markets for other flexible loads
433 offering DR. The methodology developed in this study is applicable for any
434 market participant offering load curtailment either as an individual or a popu-
435 lation of flexible loads. Reduced aggregation, a smaller number of loads offer-
436 ing larger individual curtailment, is likely to significantly improve the benefit
437 case for individual participants.

438 4.2. *What is the impact of the uncertainty distribution?*

439 The impact of environmental uncertainty can be seen in Fig. 5, which shows
440 the intraday revenue that is generated in each of the environmental uncertainty
441 distribution cases considered (cf. Fig. 3). It can be seen that there is a clear
442 difference between the cases considered. This can be accounted for by the dif-
443 ference in the expected curtailment across the cases. The extreme case has the
444 lowest expected demand response resource, and correspondingly the lowest
445 expected revenue. Thus, it can be expected that the larger the variation in time
446 of the demand response resource, the lower the revenue that can be generated.
447 This study leads to the conclusion that the uncertainty distribution of demand

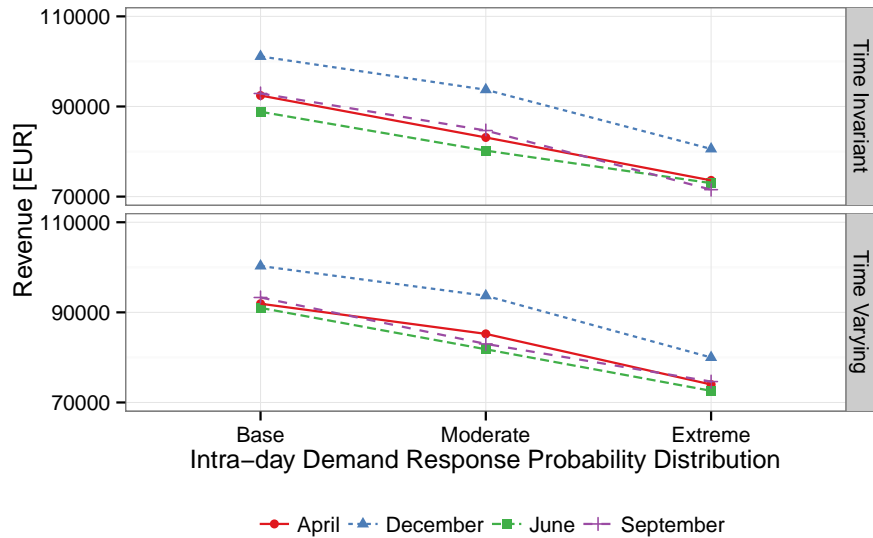


Figure 5: Expected revenue from trading on the intraday market for each of six DR uncertainty distributions.

448 response has a noticeable impact on the revenue that can be accrued through
 449 participation on the intraday market. Consequently it is imperative that uncer-
 450 tainty in achievable response be considered when evaluating the business case
 451 of DR and it is not simply assumed that the resource is perfectly responsive
 452 at all times.

453 4.3. Is it necessary to consider the temporal structure of the uncertainty distribution?

454 The impact of intraday demand response forecast accuracy is addressed in
 455 Fig. 6. In the cases illustrated here, the trading was conducted employing time
 456 invariant demand response forecasts, and the revenue was validated by ap-
 457 plying the time varying distributions to the scheduled load curtailment. The
 458 resulting revenue is compared to the outcome if trading was conducted using
 459 the time varying forecasts. The revenue difference shown in the figure corre-
 460 sponds to trading with an accurate forecast minus trading with an inaccurate
 461 forecast. It can be seen in some cases, that the inaccurate forecast actually im-

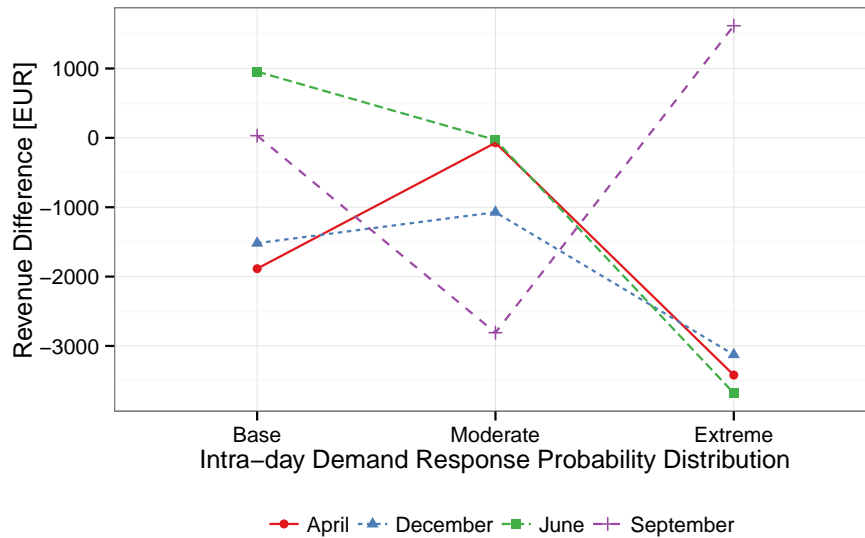


Figure 6: Revenue difference when a time invariant DR forecast is employed in the trading while the realised curtailment exhibits the time varying uncertainty distribution.

462 proves the revenue outcome, however there is no clear trend and in all cases
 463 the change in revenue is under 4%. The inaccurate forecast does not include in-
 464 formation on the temporal structure of the load curtailment that is expected as
 465 it represents the time averaged probabilities from the time varying uncertainty
 466 distribution. Consequently, approximately 50% of the time, the expected load
 467 curtailment under the inaccurate forecast will exceed that with the accurate
 468 forecast. This results in cases where some intraday trades will be accepted sub-
 469 ject to the inaccurate forecast which would not be accepted were the accurate
 470 forecast available. Similarly, some trades are accepted under the accurate fore-
 471 cast that are not accepted with the inaccurate forecast.

472 Analysis of the revenue breakdown for each of the cases considered reveals
 473 that the trade revenues with both accurate and inaccurate demand response
 474 forecasts are very similar, with most of the revenue difference resulting from
 475 changes to imbalance costs. This can be accredited to the all-or-nothing nature
 476 of the intraday trades. Slight changes to the expected achieved curtailment

477 may not affect the decision to accept a particular trade as the revenue associ-
478 ated with accepting the trade far exceeds the imbalance penalty that will be im-
479 posed if the achieved curtailment deviates a small amount from that required
480 to fulfil the trade. The use of out-of-sample regulating prices in the revenue
481 calculation contributes to the lack of trend in Fig. 6.

482 This result supports the conclusion that the intraday market is a suitable
483 trading platform for demand response. The absence of an accurate forecast
484 of the demand response resource does not preclude profitable trading on this
485 market due to the structure of its trades. Furthermore, the burden of achiev-
486 ing an accurate forecast is reduced as this study has revealed that it is not
487 strictly necessary to capture the temporal structure of the uncertainty distribu-
488 tion. However, this conclusion is sensitive to the definition of the DR resource.
489 In the cases studied, the magnitude of the load curtailment is comparable to
490 the size of a single or small number of intraday market trades. Should the
491 magnitude of the available curtailment greatly exceed the size of the trades
492 offered on the intraday market, it would be preferable to have an improved
493 forecast of the achievable curtailment so that the optimal combination of con-
494 current trades can be accepted. This indicates that while the initial deployment
495 of small-scale DR is reasonably insensitive to forecast accuracy, as the resource
496 is further deployed forecasts will play an increasingly important role.

497 **5. Conclusions**

498 This work presents optimal trading strategies for aggregated DR offering
499 load curtailment on the day-ahead and intraday markets under uncertainty.
500 A thorough analysis of the impact of DR uncertainty on revenue outcomes is
501 presented.

502 Analysis has revealed that despite significant DR uncertainty at long hori-
503 zons, trading on the day-ahead market prior to trading on the intraday market
504 is preferable to solely trading intraday. Consideration of the temporal struc-
505 ture of the demand response uncertainty when trading intraday was found

506 to be unnecessary to ensure a profitable outcome, indicating that advanced
507 forecast products are not necessary for profitable trading on this market when
508 the resource scale is comparable in magnitude to the intraday trades offered.
509 However, if the resource scale increases significantly it is likely that forecast
510 accuracy will be central to maximising revenue.

511 The key outcome of this work is that the uncertainty of load curtailment
512 has a significant impact on the revenue that can be generated through trade on
513 competitive electricity markets. Consequently, a continuation of this research
514 agenda should focus on identifying accurate uncertainty distributions for load
515 curtailment to support a comprehensive assessment of the value offered by this
516 novel power system resource.

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