

Online Adaptive Clustering Algorithm for Load Profiling

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Abstract

With the large scale deployment of smart metering, energy sector is facing ‘Big Data’ related challenges. While metered customers generate streams of data, load profiling methods are not taking advantage of this structure. Indeed, insights on the demand are traditionally provided by static typical load profiles. Renewable energy sources generate intermittency in the production and subsequently uncertainty in aligning the generation to the demand at any time. This work proposes a new view on load profiling that takes benefit of the stream structure of the data, an adaptive and recursive clustering method that generates typical load profiles updated to newly collected data. The online adaptive clustering algorithm is based on an online K-means approach using a dynamic time warping based distance associated with a facility location to adjust the number of typical load profiles. The performance of the algorithm is evaluated on a synthetic dataset and applications are presented on real world dataset from both electricity and central district heating.

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Keywords: Clustering, load profiling, smart grid, time-series analysis.

1. Introduction

The energy sector is following the trends of Big Data and growing interest is placed in collecting and analyzing energy data. The development of Advanced Metering Infrastructure (AMI), and Information and Communication Technologies (ICT), thanks to public investments (Third Energy Package in Europe [1] and the American Recovery and Reinvestment Act in the United States of America [2]), constitutes the informational backbone of the energy sector. These investments were motivated by the implementation of ‘greener’ energy policies supporting the use of larger amount of Renewable Energy Sources (RES). RES are known to introduce intermittency in the production, hence, if no actions are taken, the larger the share of RES in the generation, the farther it can be from the consumption. It is then a necessity to have information about the demand status at a resolution that allows operators to take actions to minimize the use of conventional energy sources.

Typical load profiles, that describe the consumption of group of customers, are used to provide information to the utilities about the demand status. Load profiles have been mainly used in the electricity sector, but other energy fields (e.g. central district heating, gas) can benefit from its development. The Electricity sector is also the main leverage in transitioning to more sustainable energy production/consumption providing the highest share of RES. As production has to meet the consumption at any time, RES intermittency has to be compensated on the consumption side. Solutions

24 exist to optimize the use of RES (i.e. storage, demand side management)
25 but they all rely on precise information on generation and demand statuses.

26 Typical load profiles were traditionally generated for the electricity sector
27 by segmenting customers by activities. With only a few customers metered,
28 demographics or customers categories available, the goal was to estimate load
29 profiles of non-metered customers, using assumptions to extrapolate hourly
30 load profiles from yearly consumption. It was known to be inaccurate as sub-
31 populations exist in almost each category [3]. Deployment of AMI has drastically
32 changed the paradigm of load profiling from estimating the demand
33 using a few metered customers to summarizing the information contained in
34 a large pool of metered customers.

35 State-of-the-art load profiling methods use clustering algorithms combined
36 with dimension reduction techniques on batches of historical data and
37 generate static typical load profiles which suppose that loads are repeated
38 over years taking into account seasonality and other temporal periodicity of
39 the data [4, 3, 5, 6, 7]. This is a first step toward data-driven load profiling.
40 Nevertheless, technological evolution of white appliances and the penetration
41 of new type of electrical appliances (e.g. electric vehicle, heat pumps,
42 batteries) are actually changing the loads on a time scale which requires
43 the profiling to be rerun more often. A recursive approach to load profiling
44 would be a computationally inexpensive way to do so. The problem
45 of temporal dependence, inherent to time series, has been tackled by using
46 Wavelet transform [8] or Fourier transform [9] that can be seen as dimension
47 reduction techniques. However, both the number of clusters and the
48 assignment of customers to a cluster remain static and the clustering has

49 to be rerun to be updated with newly collected data. Bayesian framework
 50 is by essence inferential and is a solution to the problem of updating the
 51 clusters to newly collected data. Example of Gaussian mixture models [10]
 52 and Dirichlet process [11] can be found in the literature but none of them
 53 challenges the temporal static structure of the clustering.

Table 1: The different type of clustering-based load profiling [12].

number of clusters:	static	dynamic
load static	Type 1	Type 2
load dynamic	Type 3	Type 4

54 Benítez *et al.* have defined four types of clustering-based load profiling
 55 (Table 1) depending on whether loads are considered dynamic or static and
 56 whether the number of clusters K is evolving or not. In this categorization,
 57 the work in [5, 6, 7, 8, 9, 10, 11] are Type 1. In their latest works, Benítez
 58 *et al.* have implemented type 2 [12] and type 3 [13] clustering-based load
 59 profiling. In this paper, we present a Type 4 clustering-based load profiling
 60 methodology. The clustering process is i) flexible, customers can change
 61 cluster ; ii) adaptive, the number of clusters can change according to data
 62 structure; iii) online, the typical load profiles are dynamic and recursively
 63 updated and iv) it respects time dependency of load patterns.

64 The remainder of this paper is organized as follow: Section 2 presents the
 65 notations and the preprocessing of the data, the methodology is introduced in
 66 Section 3, the performance of the online adaptive clustering is evaluated on a
 67 synthetic data set in Section 4. Real-world data applications are presented in
 68 Section 5 and the work is ultimately concluded with an outlook in Section 6.

69 **2. Preliminaries: Notations and Data Preprocessing**

70 The notations used to present the online adaptive clustering algorithm
 71 in the following sections are first introduced. Smart meters can record con-
 72 sumption at high frequency (up to 1 second), however data are broadcast
 73 into batches at regular intervals during a day to minimize the communica-
 74 tion costs. In this framework, metering data are then not collected online
 75 but as blocks of data Ω^t of fixed length (e.g. days, weeks). Each block Ω^t ,
 76 $t \in \{0, \dots, T\}$ consists into a set of vectors

$$\Omega^t = \{\mathbf{X}_1^t, \dots, \mathbf{X}_i^t, \dots, \mathbf{X}_I^t\}, \quad (1)$$

77 where each vector \mathbf{X}_i^t is a load from meter i at time step t with all the same
 78 length (e.g. 24 for blocks of a day with hourly resolution). The set of typical
 79 load profiles Υ^t generated after clustering Ω^t at step t is formed by K^t vectors

$$\Upsilon^t = \{\mathbf{Y}_1^t, \dots, \mathbf{Y}_k^t, \dots, \mathbf{Y}_{K^t}^t\}, \quad (2)$$

81 where K^t is the number of clusters at time step t . The clustering algorithm
 82 used in this work is distance-based. The distances between the set of loads
 83 Ω^t and the typical load profiles Υ^{t-1} at previous time step $t-1$ are calculated
 84 and stored into a matrix

$$\mathbf{D}^t = d(\Omega^t, \Upsilon^{t-1}) = \begin{bmatrix} d_{11}^t & \dots & d_{1k}^t & \dots & d_{1K^t}^t \\ \vdots & \ddots & & & \vdots \\ d_{i1}^t & & d_{ik}^t & & d_{iK^t}^t \\ \vdots & & & \ddots & \vdots \\ d_{I1}^t & \dots & d_{Ik}^t & \dots & d_{IK^t}^t \end{bmatrix}. \quad (3)$$

85 The distance between a load \mathbf{X}_i^t and a typical load profile \mathbf{Y}_k^{t-1} is noted d_{ik}^t .
 86 A vector of labels $\mathbf{A}^t = [A_1^t, \dots, A_I^t]$ specifying to which typical load profile k
 87 each individual load \mathbf{X}_i^t in Ω^t is assigned to is generated using the operator,

$$\forall i \in [1, I], A_i^t = \underset{k}{\operatorname{argmin}}(\mathbf{d}_i^t) \quad (4)$$

88 on each line \mathbf{d}_i^t of matrix \mathbf{D}^t . The result of assigning each load to a typical
 89 load profile is a partition of the loads $\Pi^t = \{\mathbf{P}_1^t, \dots, \mathbf{P}_k^t, \dots, \mathbf{P}_{K^t}^t\}$. As an
 90 example, we define a set of five loads $\{\mathbf{X}_1, \dots, \mathbf{X}_5\}$, and a possible partition
 91 into two clusters could be, $\Pi = \{\mathbf{P}_1 = \{\mathbf{X}_1, \mathbf{X}_3, \mathbf{X}_4\}, \mathbf{P}_2 = \{\mathbf{X}_2, \mathbf{X}_5\}\}$.

92 If raw loads are clustered, the main information used to cluster would
 93 be the average consumption, the amplitude of the peak and the exact peak
 94 location. To make the loads comparable, the loads \mathbf{X}_i^t have to be normalized.
 95 In this work, we have opted to divide each load by their reference power (i.e.
 96 maximum consumption over the period) so that they are bounded to $[0, 1]$ [5].

97 In the remainder of this paper, the t index will be omitted to simplify the
 98 notation when objects from the same time step are used.

99 3. Proposal Clustering Algorithm

100 The splitting of this section into subsections is materialized by dotted
 101 rectangles in Figure 1. Section 3.1 explains the setting of the online clustering
 102 algorithm parameters. Section 3.2 presents the online clustering that consists
 103 into an iterative process based on the K-means algorithm that connects time
 104 steps. Section 3.3 presents the facility location approach, used to evaluate if
 105 extra cluster centers should be created.

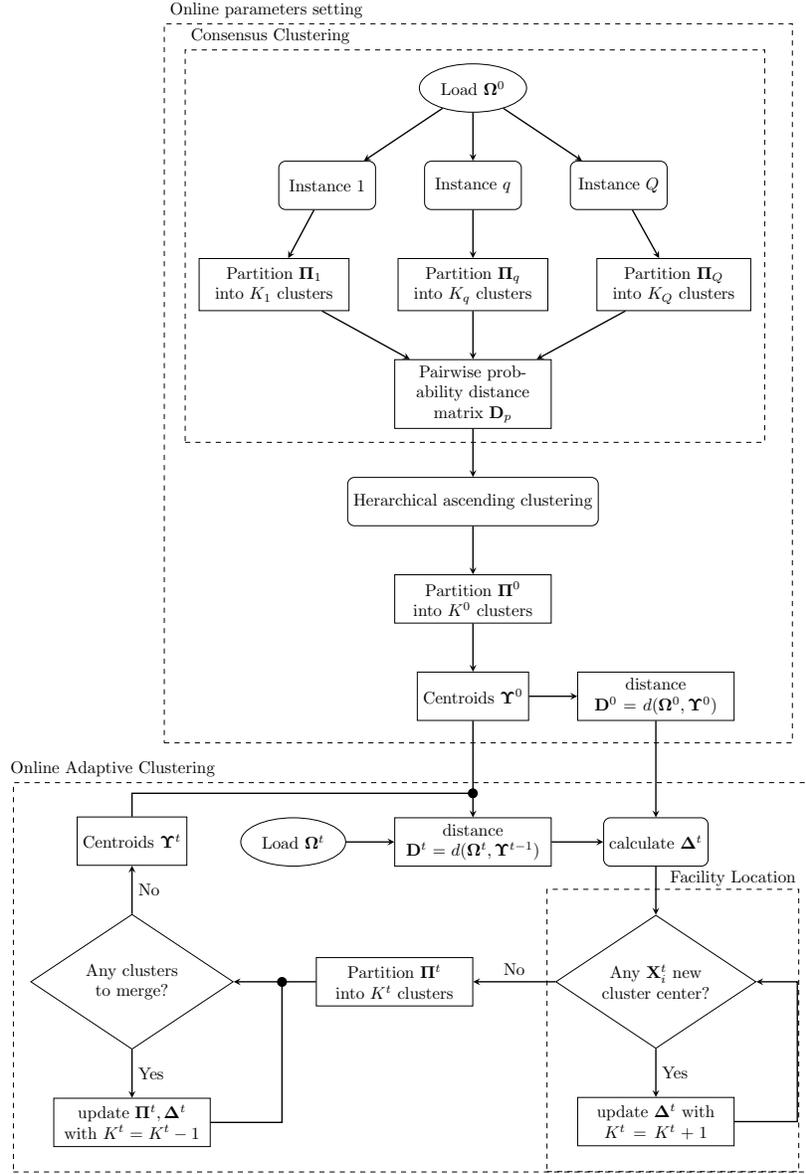


Figure 1: Overview of the online adaptive clustering algorithm.

106 *3.1. Consensus Clustering: Online parameters setting*

107 The online adaptive clustering algorithm requires three parameters: Υ^0 ,
 108 the first set of typical load profiles; K^0 , the number of cluster centers at
 109 $t = 0$ and $d(\Omega^0, \Upsilon^0)$, the distance matrix at $t = 0$. To set these parameters,
 110 available historical data can be used offline to create the first partition Π^0 .

111 Determining the optimal number of clusters K without *prior* information
 112 is a non-trivial and computationally expensive problem. The classical way
 113 to **determine** it is by running several instances, $q \in \{1, \dots, q, \dots, Q\}$, of a
 114 clustering algorithm with different values of K_q to select K^0 that minimizes
 115 a criterion [14]. Thereafter only the partition generated with the optimal
 116 K^0 is kept, the other instances being used only to determine K^0 . In this
 117 work, we opted for consensus (or ensemble) clustering to **determine** K^0 and
 118 generate a robust partition [15]. **Consensus clustering consists into running**
 119 **in parallel several instances q of clustering algorithm(s) (possibly different)**
 120 **with different values of K_q that return q partitions Π_q of historical data**
 121 **Ω^0 . Every instance contributes to determine K^0 , the partition Π^0 and the**
 122 **cluster centroids Υ^0 .** From the partitions $\{\Pi_1, \dots, \Pi_q, \dots, \Pi_Q\}$ a probability
 123 distance \mathbf{D}_p is calculated,

$$\mathbf{D}_p(i, l) = 1 - \frac{\sum_{q=1}^Q K_q \delta(\mathbf{A}_{qi}, \mathbf{A}_{ql})}{\sum_{q=1}^Q K_q}, \quad (5)$$

$$\text{with } \delta(a, b) = \begin{cases} 1, & \text{if } a = b \\ 0, & \text{if } a \neq b \end{cases} \quad (6)$$

124 δ the co-occurrence matrix specifies if two points are in the same cluster in
 125 each instance and creates a linkage between each pair of loads in Ω^0 . The
 126 sum of the co-occurrence matrices is weighted by the number of clusters K_q

127 set in each instance. The benefits of consensus clustering are multiple; all
 128 instances are used to build the probability distance matrix; the final partition
 129 is a consensus between the different instances so it reduces the bias of each
 130 instance; it gets freed from a potential bias due to the choice of initial set of
 131 cluster centers.

132 Using the dendrogram of the hierarchical ascending clustering imple-
 133 mented on the probability distance matrix with the Ward criterion, the user
 134 determines the number of clusters K^0 . The expertise of the user in solving
 135 a specific problem is necessary to determine the optimal number of clusters
 136 K^0 . From the K^0 clusters, the initial typical load profiles, Υ^0 are calcu-
 137 lated by the average of the loads in each cluster, and the initial distance
 138 matrix $\mathbf{D}^0 = d(\Omega^0, \Upsilon^0)$ of each loads in Ω^0 to the typical load profiles Υ^0 is
 139 generated.

140 3.2. Online Clustering

141 The online clustering algorithm takes as input the results of the consen-
 142 sus clustering, the typical load profiles Υ^0 and \mathbf{D}^0 the matrix of distances
 143 between the loads in Ω^0 and Υ^0 (Figure 1). The time iterative process of
 144 the online clustering uses the core of K-means algorithm with:

- 145 • An assign step, where loads in Ω^t are assigned to the closest centroid
 146 in Υ^{t-1} ,
- 147 • Update centroids by averaging loads in each cluster.

148 It differs from K-means algorithm in using exponential smoothing to transfer
 149 structural information from previous time steps during the calculation of the

150 distance matrix,

$$\Delta^t = \frac{\sum_{\tau=0}^t \lambda^{t-\tau} \mathbf{D}^\tau}{\sum_{\tau=0}^t \lambda^\tau} \quad (7)$$

151 λ is the exponential smoothing coefficient and takes a value in $[0, 1]$, which
 152 corresponds to how much of the previous time step information is transmitted
 153 to the next one. The assignment of the loads in Ω is based on matrix Δ .
 154 Implementation of the exponential smoothing relies on the assumption that
 155 loads are relatively stable and those grouped in a same cluster may exhibit
 156 the same dynamic over time and thus remain together.

157 The centroids are updated by averaging the loads $\mathbf{X}_i^t \in \mathbf{P}_k^t$. Hence the
 158 most recent data are used in the calculation of the typical load profiles which
 159 provides up-to-date typical load profiles.

160 Consumption data display time-dependency. The clustering process pre-
 161 sented in this work is distance-based, so the distance definition chosen should
 162 respect time dependency and create clusters based on pattern. Several dis-
 163 tance measures using correlation coefficients, Euclidean distance and Dy-
 164 namic Time Warping (DTW) have been used in clustering time series [16, 17].
 165 To tackle this problem, we suggest to use a dissimilarity index [18],

$$d(\mathbf{X}, \mathbf{Y}) = \phi[\rho(\mathbf{X}, \mathbf{Y})]d_{DTW}(\mathbf{X}, \mathbf{Y}) \quad (8)$$

166 that balance a first order temporal correlation coefficient

$$\rho(\mathbf{X}, \mathbf{Y}) = \frac{\sum_{m=1}^{M-1} (x_{m+1} - x_m)(y_{m+1} - y_m)}{\sqrt{\sum_{m=1}^{M-1} (x_{m+1} - x_m)^2} \sqrt{\sum_{m=1}^{M-1} (y_{m+1} - y_m)^2}}, \quad (9)$$

167 estimating the dynamic behaviors and the DTW distance

$$d_{DTW}(\mathbf{X}, \mathbf{Y}) = \min_{r \in M} \left(\sum_{(i,j) \in \{1, \dots, M\}^2} |x_i - y_j| \right), \quad (10)$$

168 for any given load \mathbf{X} and typical load profile \mathbf{Y} of same length M using the
 169 function ϕ

$$\phi(u) = \frac{2}{1 + \exp(u)}, \quad (11)$$

170 an adaptive tuning function to balance automatically the distance d_{DTW} ac-
 171 cording to the temporal correlation coefficient ρ [19]. DTW has been broadly
 172 used in time series analysis and pattern recognition, it measures temporal
 173 similarities between time series. It calculates the Euclidean distance between
 174 a point of a time series and all the points of the other time series to create
 175 a distance matrix between each pair of points. It then finds the shortest
 176 way r from the lower left corner to the upper right corner which is called a
 177 warping path. We used the Paliwal window [20] to limit the shifting to only
 178 a few time steps (i.e. a window around the diagonal of the distance matrix)
 179 depending on the data resolution and to speed up the calculation.

180 3.3. *Adaptivity: Semi-Online Facility Location*

181 So far the algorithm is only online, but not yet adaptive. In this section,
 182 we present a probabilistic approach called facility location to adjust the num-
 183 ber of clusters according to new unseen data [21]. When clustering loads,
 184 two antagonist processes have to be handled:

- 185 • Stability: loads changing shape simultaneously (e.g. seasonality) should
 186 stay in the same cluster,
- 187 • Novelty: disruptive load behavior should generate a new cluster center.

188 Facility location tackles the second point. A cost C_i^a is set to the assignment
 189 of each load, which is proportional to the distance d_{i,A_i} of each load \mathbf{X}_i^t to

190 the closest typical load profile $\mathbf{Y}_{A_i}^{t-1}$ and a cost C^f to the creation of a new
 191 facility (i.e. cluster center) with $C^f \gg C_i^a$. C_i^a and C^f are combined to form
 192 a probability

$$p(\mathbf{Y}_{k+1}=\mathbf{X}_i)=\min\left(\frac{C_i^a}{C^f},1\right), \quad (12)$$

193 that a load becomes a new cluster center. Hence the larger d_{i,A_i} , the larger
 194 the marginal cost C_i^a of adding a new load to existing clusters, the higher
 195 the probability that it becomes its own cluster center. The facility cost is
 196 regulating the clusters' size and can be empirically chosen according to the
 197 clusters size wanted.

198 As the newly generated loads arrive simultaneously in a block Ω , facility
 199 location is implemented in a semi-online way and evaluates the creation of
 200 new cluster centers on Ω instead of a load at a time as in the completely
 201 online setup [22]. A threshold γ_{min} is defined to set how many loads should
 202 exhibit a disruptive behavior to generate an extra typical load profile, thus
 203 sensitivity to outliers is reduced. Monte-Carlo simulations are run 1000 times
 204 to obtain the distribution of the number of loads above the threshold, and
 205 the mode of the distribution is used to evaluate if the threshold is reached
 206 or not. Hence it makes the algorithm consistent. If the threshold is reached,
 207 the load which is the farthest from its closest centroid is used as extra cluster
 208 center and the distance matrix \mathbf{D} is then recalculated to check if other loads
 209 in Ω should be assigned to the new typical load profile. Thereafter Δ is also
 210 updated with $K+1$ clusters (Figure 1).

211 If two cluster centers are converging, the algorithm would ultimately
 212 merge them, but it would take many iterations. To avoid redundant typ-
 213 ical load profiles, a minimum threshold $d_{min} < d(\mathbf{Y}_m, \mathbf{Y}_n)$ between two cluster

214 centers m and n is defined. If a pair of centroids gets under d_{min} , they are
 215 considered similar and are merged to form a single cluster with the average
 216 of their assigned loads as centroid. Thereafter Δ is also updated with $K-1$
 217 clusters (Figure 1). Hence the algorithm reacts faster to decreasing number
 218 of typical load profiles over time.

219 3.4. Setting the parameters

220 The online adaptive clustering algorithm requires setting parameters em-
 221 pirically as the nature of the data (e.g. electric load data, central heating
 222 district data), the resolution, the preprocessing affect the clustering process.
 223 Moreover the objective of the clustering can differ from one application to
 224 another, which is why the setting of the parameters is left to the user. Table 2
 225 gives guidelines on the action of each parameter on the clustering process.

Table 2: Influence of the parameters on the clustering process.

Parameter	Definition	Value	Influence
K^0	Initial number of cluster centers	$n \in \{2, \dots, N\}$	On the first iterations
λ	Exponential forgetting	$[0, 1]$	Smooth the clustering
C^f	Facility cost	relative to C^a	Size (radius) of the clusters
d_{min}	Minimum distance between cluster centers	Relative to the expected number of clusters	size (radius) of the clusters
γ_{min}	Number of disruptive load needed to create a new cluster	$n \in \{2, \dots, 10\}$	Limits fluctuations of K

226 Setting K^0 has influence only on the few first iterations (depending on λ)
 227 as the initial structure will fade out progressively thanks to the exponential
 228 forgetting. λ is influencing how much structural information is transfered
 229 from one iteration to another, the larger λ the more information transmitted.

230 C^f and d_{min} are parameters controlling the adaptivity and more precisely
 231 controlling the radius of the clusters. A large value of C^f will allow larger
 232 clusters and thus a smaller K . A small value of d_{min} will allow the creation
 233 of smaller clusters and thus a larger K . γ_{min} can be used to limit fluctuation
 234 of K .

235 4. Online Adaptive Clustering Performance Evaluation Using Sim- 236 ulated Data

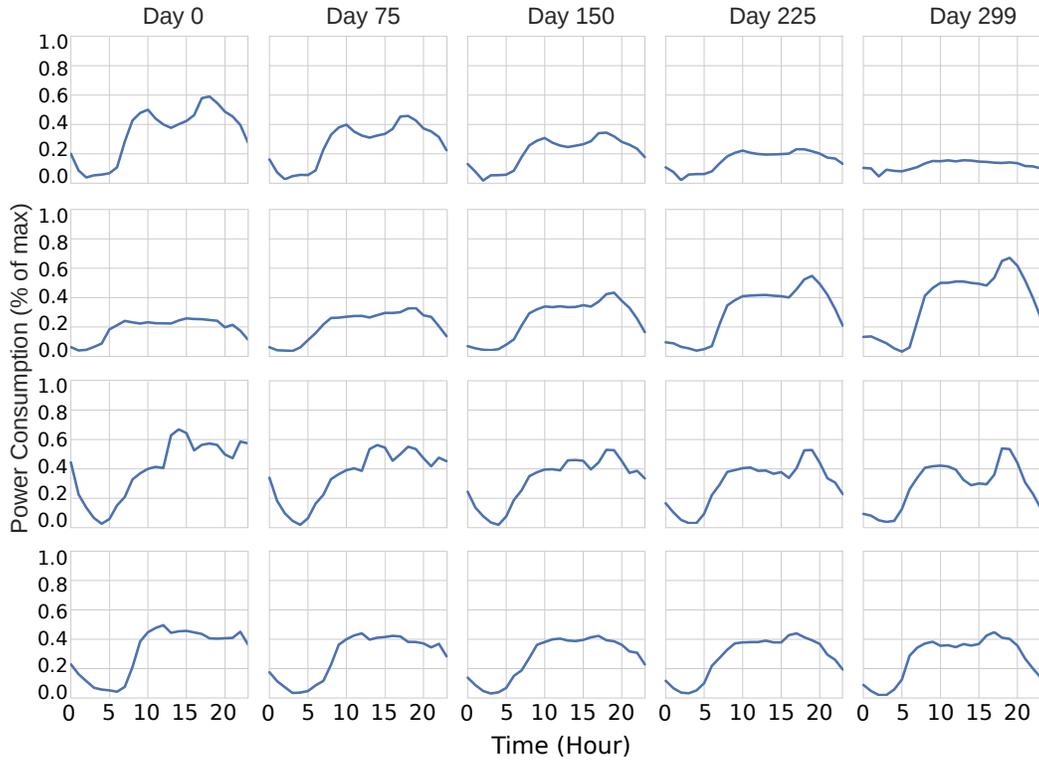
237 The performance of the online adaptive clustering algorithm is first eval-
 238 uated on a synthetic dataset where the true typical load profile for each con-
 239 sumer is known. The following section describes how synthetic loads were
 240 generated, how the clustering process was evaluated and presents the results.

241 4.1. Data Generation

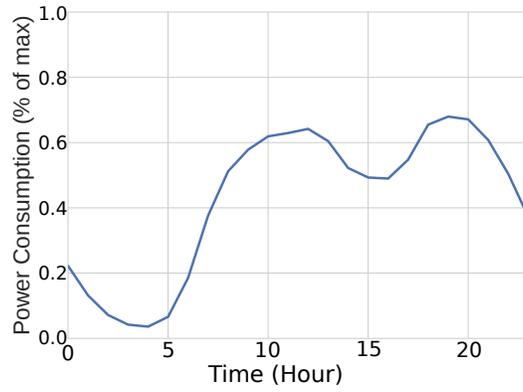
242 The following **simulation** aims at demonstrating that the proposed algo-
 243 rithm can both handle slow changing typical load profiles as well as disruptive
 244 behaviors (i.e. unobserved in the previous steps). To do so four slow chang-
 245 ing and one disruptive typical load profiles are created based on nine typical
 246 load profiles from ENTSO-E data base displaying different load behaviors
 247 at hourly resolution [23]. The four slowly changing typical load profiles are
 248 generated using four pairs of typical load profiles from ENTSO-E. The daily
 249 typical load profiles \mathbf{Y}_k are synthetically created as weighted averages

$$\mathbf{Y}_k^t = \left(1 - \frac{t}{300}\right) \mathbf{Y}_k^0 + \frac{t}{300} \mathbf{Y}_k^{299} \quad (13)$$

250 of \mathbf{Y}_k^0 and \mathbf{Y}_k^{299} respectively the starting (Day 0) and ending (Day 299) pro-
 251 files exhibited by typical load profile k . Figure 2(a) presents the evolution



(a)



(b)

Figure 2: Synthetic data generation based of ENTSO-E load profiles. Morphing of the four typical load profiles (a) and the new load behavior appearing at day 200 (b).

252 of these typical load profiles. From the four slow changing typical load pro-
 253 files, 1000 individual daily loads are sampled. Each of the 1000 simulated
 254 customers is randomly assigned to one of the four slow changing typical load
 255 profiles $\Upsilon = \{\mathbf{Y}_1, \dots, \mathbf{Y}_4\}$. The simulated daily loads

$$\mathbf{X}_i^t = \mathbf{Y}_k^t + \mathcal{N}(0, \Sigma) \quad (14)$$

256 are sampled from the typical load profiles \mathbf{Y}_k^t by adding a multivariate Gaus-
 257 sian noise $\mathcal{N}(0, \Sigma)$. The covariance matrix

$$\Sigma = \begin{bmatrix} \sigma_1^2 \rho_{11} & \dots & \sigma_1 \sigma_l \rho_{1m} & \dots & \sigma_1 \sigma_M \rho_{1M} \\ \vdots & \ddots & & & \vdots \\ \sigma_l \sigma_1 \rho_{l1} & & \sigma_l^2 \rho_{lm} & & \sigma_l \sigma_M \rho_{lM} \\ \vdots & & & \ddots & \vdots \\ \sigma_L \sigma_1 \rho_{L1} & \dots & \sigma_L \sigma_m \rho_{Lm} & \dots & \sigma_L^2 \rho_{LM} \end{bmatrix} \quad (15)$$

258 is stochastically generated. $\sigma = \{\sigma_1, \dots, \sigma_{24}\}$ is a normalized random vector of
 259 standard deviation and ρ is a matrix of coefficient decreasing exponentially
 260 from the diagonal

$$\rho_{lm} = \exp\left(\frac{-|l-m|}{\tau}\right), \quad (16)$$

261 which adds some small time shifting to the patterns. The daily load data
 262 were then normalized to $[0,1]$ by dividing them by their reference power.

263 At time step 100, 250 of the 1000 customers generated disrupt from their
 264 slow transitioning typical load profile to the fifth typical load profile (Fig-
 265 ure 2(b)). The number of clusters is in the same time expected to change
 266 automatically, generating an extra cluster center which groups the 250 dis-
 267 ruptive loads. At time step 200, the 250 customers are catching back their

268 original slow transitioning typical load profiles. The number of clusters is
 269 then expected to change from five to four clusters and reassigning the loads
 270 to the cluster corresponding to their original typical load profile.

271 4.2. Performance Evaluation

272 The performance of the algorithm is evaluated using the Normalized Mu-
 273 tual Information (NMI) which is a criterion based on entropy and cross-
 274 entropy as defined in information theory. It actually evaluates how much
 275 information is shared between two vectors of labels. The entropy

$$H(\mathbf{U}) = \sum_{i=1}^I p(u_i) \log(p(u_i)), \quad (17)$$

276 is the amount of disorder in vector \mathbf{U} where each element can take a value
 277 in $\{u_1, \dots, u_I\}$ and the probabilities $p(u_i)$ represent the probabilities that an
 278 object picked at random from \mathbf{U} has value u_i . The Mutual Information (MI)

$$MI(\mathbf{U}, \mathbf{V}) = \sum_{i=1}^I \sum_{j=1}^J p(u_i, v_j) \log \left(\frac{p(u_i, v_j)}{p(u_i)p(v_j)} \right) \quad (18)$$

280 is basically the entropy of the joint probability between vector of labels
 281 $\mathbf{U} = \{u_1, \dots, u_I\}$ and $\mathbf{V} = \{v_1, \dots, v_J\}$. In the context of this work, the joint prob-
 282 ability $p(\mathbf{Y}_j, \mathbf{\Pi}_k)$ is the probability that a load is both from typical load
 283 profile \mathbf{Y}_j and assigned to cluster $\mathbf{\Pi}_k$. MI is then normalized,

$$NMI(\mathbf{U}, \mathbf{V}) = \frac{MI(\mathbf{U}, \mathbf{V})}{\sqrt{H(\mathbf{U})H(\mathbf{V})}} \quad (19)$$

284 and takes value in $[0, 1]$ where 1 is a perfect match between \mathbf{U} and \mathbf{V} .

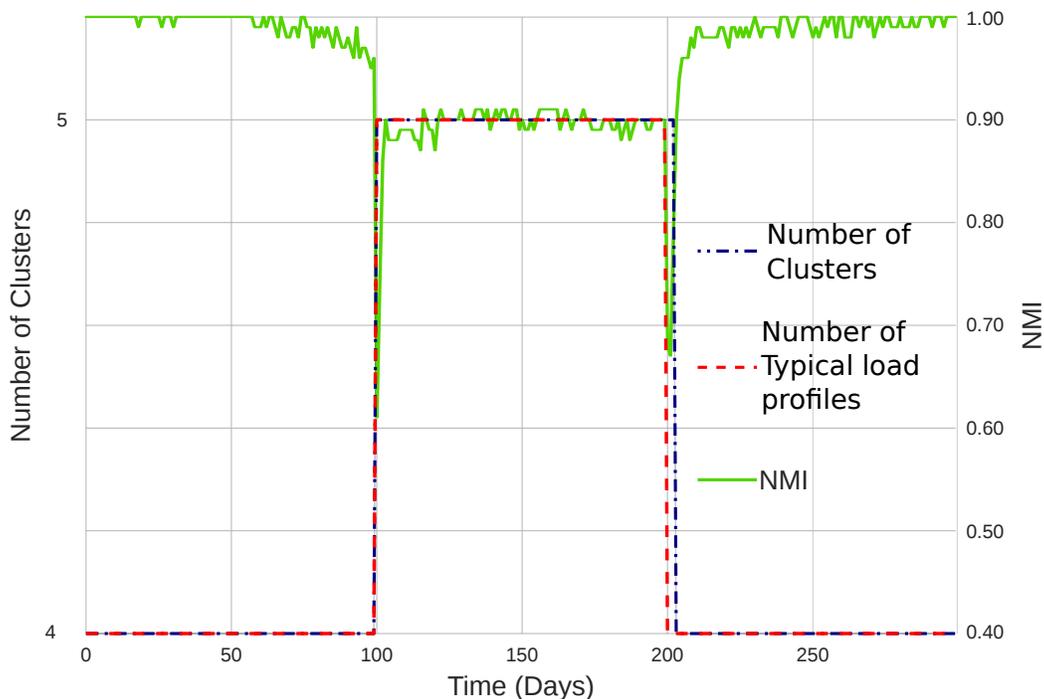


Figure 3: mode of the NMI and the number of clusters over the test period.

285 *4.3. Online Clustering Setup and Results*

286 The evaluation focuses on the online adaptive clustering algorithm. Hence
 287 the consensus clustering is not performed on the synthetic data and the first
 288 partition Π^0 is actually the real assignment of the customers to typical load
 289 profiles in Υ . The facility cost is fixed to $C^f=100$, the number of points γ_{min}
 290 required to generate a new cluster is set to one, the exponential smoothing
 291 is $\lambda=0.85$ and the minimum distance between cluster centers is $d_{min}=0.07$.

292 The results of the analysis are presented in Figure 3 with the evolution
 293 of the number of clusters (blue dotted line) and the NMI (green solid line)
 294 over the test period. The number of typical load profiles used to sample the
 295 daily load curves is displayed with a red dashed line. It shows that the num-

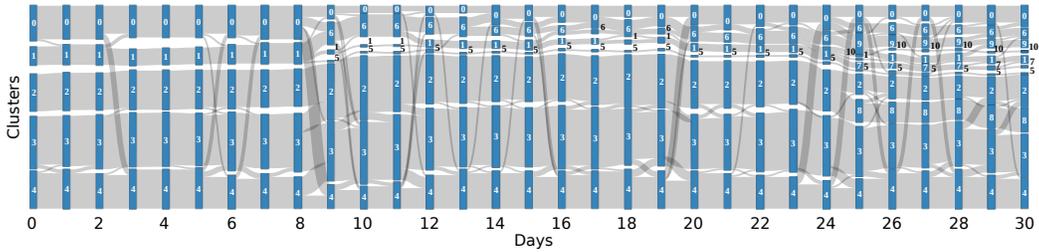


Figure 4: Sankey graph displaying the flow of buildings in the different clusters from one day to another during the test period.

296 ber of clusters generated by the online adaptive clustering algorithm follows
 297 precisely the number of typical load profiles until day 200. Even when at
 298 time step 100, the number of typical load profiles is changing from four to
 299 five. When the number of typical load profiles used to sample the loads is
 300 decreasing from **five to four**, we observe a delay of 2 days before the algo-
 301 rithm adjusts the number of clusters. Besides detecting correctly the number
 302 of clusters until day 100, the algorithm groups correctly the loads that are
 303 sampled from the same typical load profile in the same cluster as the NMI
 304 stays close to 1.0 until day 50. At day 50, a decrease of the NMI is observed.
 305 This can be explained by the real partition information provided at $t=0$ fading
 306 away in the exponential smoothing as well as a convergence of the typical
 307 load profiles (see Figure 2) which can engender some misclassifications. At
 308 day 100, we observe a drop to approximately 0.6 and the NMI comes quickly
 309 back to around 0.9 in the next day and oscillate around 0.9 until day 200. At
 310 day 200, the NMI drops again down to 0.75 and comes quickly back to 0.95
 311 the next day and continues to increase until it oscillates between 0.99 and
 312 1.0. At the end of the test period, the algorithm classifies correctly the loads
 313 despite the change from four to five and back to four typical load profiles.

314 The online adaptive clustering performed accurately on the synthetic
315 dataset as it generates the correct number of clusters and groups correctly
316 customers generated from the same typical load profile in the same cluster.

317 5. Applications to **Real-world Data**

318 The online adaptive clustering algorithm has been tested on two real-
319 world datasets, i) central district heating loads from 97 buildings in Copen-
320 hagen at hourly resolution for a month, ii) 13241 electrical loads **from indus-**
321 **tries, businesses and households with PV (i.e. for billing purposes)** at hourly
322 resolution for an entire year. They exhibit different characteristics which can
323 be observed when profiling loads and demonstrate a wider range of applica-
324 tions of the online adaptive load profiling clustering to energy systems. **The**
325 **code of the online adaptive clustering algorithm has been made available on**
326 ***GitHub*¹ to the interested reader.**

327 5.1. *Central District Heating Data*

328 HOFOR, the operator of the central district heating in Copenhagen area,
329 provided data from 97 building over a period of a month (31 days in Mach-
330 April) with hourly resolution. A block Ω groups a day of data ($M=24$) and
331 no preprocessing has been operated on the data as the consumptions are all
332 of the same magnitude $[0,1]$.

333 The consensus clustering is using a modified version of the K-means algo-
334 rithm that uses d_{DTW} as a distance metric and is applied with $K_q=\{2,\dots,10\}$

¹<https://github.com/gleray/Online-Kmeans>

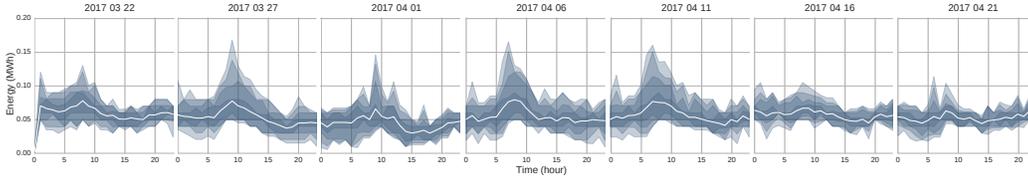


Figure 5: Evolution of cluster 4 along the test period.

335 on data generated at day 0. From the dendrogram obtained with the hier-
 336 archical ascending clustering, a partition Π^0 into five clusters is generated.
 337 The online adaptive clustering uses the centroids Υ^0 and \mathbf{D}^0 obtained from
 338 Π^0 as initial parameters and runs over 31 days.

339 The online adaptive clustering algorithm starts with $K=5$ clusters, a fa-
 340 cility cost $C^f=7.5$, it needs only one building to create a new cluster center,
 341 the exponential smoothing is $\lambda=0.85$ and the minimum distance between
 342 cluster centers is $d_{min}=0.01$. The evolution of the clusters' composition is
 343 summarized in a Sankey diagram (Figure 4) that displays the flow of cus-
 344 tomers between clusters from one day to the next. The clusters are stable
 345 over time, besides some adjustments with few buildings changing cluster at
 346 each iteration. At iteration 9, cluster 1 splits into cluster 1, 6 and 5. Cluster
 347 5 is actually a single building with a pattern different from the rest of the
 348 pool. We observe again a splitting at day 25, cluster 1 splits into cluster 1,
 349 10, 7 and cluster 9 is taking elements from cluster 1, 0 and 6. The evolution
 350 of cluster 4 is presented in Figure 5 and shows how the typical load profile's
 351 shape changes slowly over the period.

352 No predefined classification is available to assess the quality of the parti-
 353 tion, hence the number of clusters and the RMSE between individual loads
 354 and their assigned typical load profile over the test period (Figure 6) have

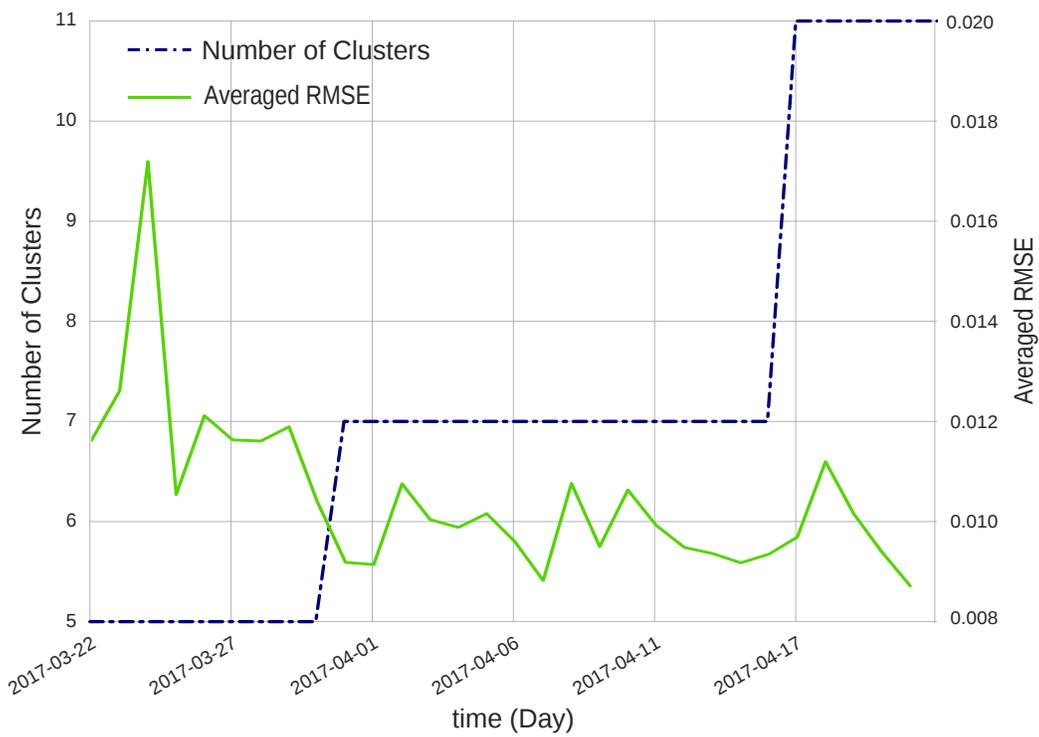


Figure 6: Number of clusters and Averaged Root Mean Square Error (RMSE) between daily loads and their assigned typical load profile over the test period for the central district heating data.

355 been used to evaluate the partition. As expected, the RMSE does not depend
 356 on the number of clusters and globally decreases over the period. It confirms
 357 first that the online adaptive clustering algorithm summarizes accurately the
 358 loads using a limited number of typical load profiles in the case of stable typ-
 359 ical load profiles; second, it is fast as it uses only one K-means iteration at
 360 each time step and last but not least it demonstrates successful application
 361 of the online adaptive clustering algorithm for profiling non electric loads.

362 *5.2. Electrical Load Data*

363 Radius, the DSO in Copenhagen area, provided the second data set. It
 364 consists of a year (240 days after removing missing data) of hourly power
 365 consumption data from $N=13241$ customers. The customers metered at
 366 hourly resolution by Radius are businesses, industries and households with
 367 PVs. The blocks Ω consist of a day ($M=24$) and the loads were preprocessed
 368 by dividing them by the peak over the period as explained in Section 2.

369 The consensus clustering is using the same modified version of the K-
 370 means algorithm presented in Section 5.1 with $K_q\{10, \dots, 100\}$ on day 0: 2015-
 371 01-12. The partition Π^0 is obtained by cutting the dendrogram into seven
 372 clusters. It is intentionally underestimating the number of clusters present
 373 in the dataset (approx. 20).

374 The online adaptive clustering algorithm starts with $K=10$ clusters cen-
 375 ters, a facility cost set to $C^f=950$, the minimum number of customers to
 376 create a new cluster center is $\gamma_{min}=5$, an exponential smoothing coefficient
 377 of $\lambda=0.85$, and a minimum distance between two cluster centers set to
 378 $d_{min}=0.13$. A standard K-means algorithm using Euclidean distance and
 379 a Self Organizing Map (SOM) applied on the entire set of daily load pro-

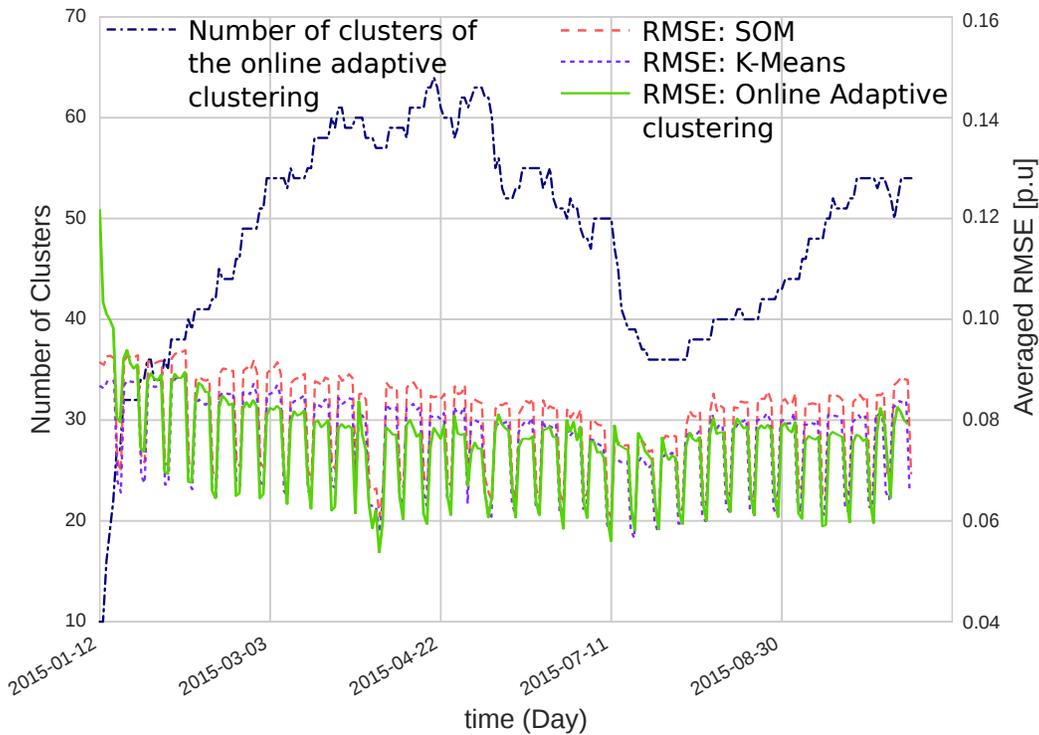


Figure 7: Number of clusters and Averaged Root Mean Square Error (RMSE) per unit of peak load, between daily loads and their assigned typical load profile over the test period for Benchmarks: SOM (7.9% RMSE overall score), K-means (7.5% RMSE overall score) and the online adaptive clustering algorithm (7.2% RMSE overall score).

380 files with $K=50$ have been used to benchmark the online adaptive clustering
 381 algorithm [5].

382 The results are presented in Figure 7 with the number of clusters and the
 383 averaged RMSE between daily loads and their assigned typical load profile for
 384 the benchmarks and the online adaptive clustering algorithm. The number of
 385 clusters generated by the online adaptive clustering algorithm first increases
 386 up to 64 around 2015-04-22 before going down to 36 during the summer and
 387 up again to 54. The averaged RMSEs show weekly periodicity which results

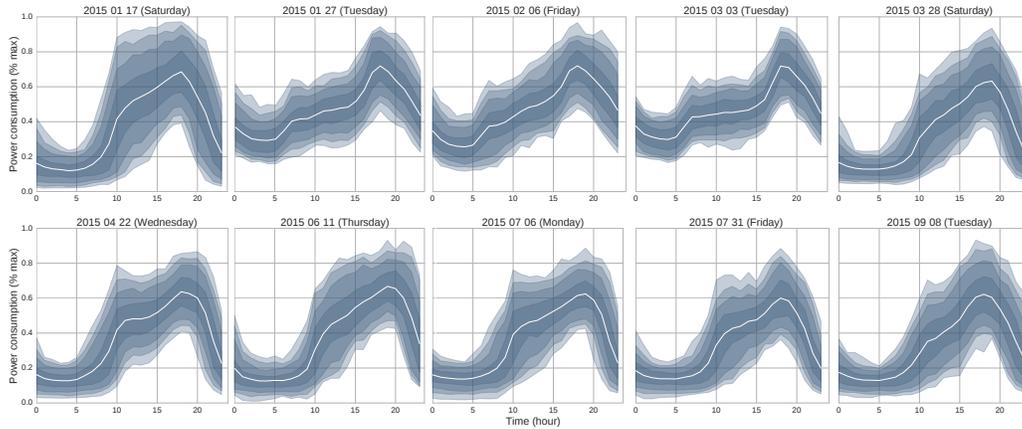


Figure 8: Evolution of cluster 15 along the test period.

388 from the customers' activity in the study, mostly industries and businesses,
 389 that are usually closed on weekends and thus displays more homogeneous
 390 patterns. The number of clusters seems to influence marginally the average
 391 RMSE of the online adaptive clustering algorithm, besides the first 14 days,
 392 which means that the algorithm is finding accurately the number of latent
 393 typical load profiles at each iteration. When the number of clusters in the
 394 online clustering algorithm gets close to 50, as set in the benchmark, the
 395 average RMSE of the benchmarks is getting closer (or equal) to the RMSE
 396 of the online adaptive clustering algorithm. The K-means actually beats the
 397 online adaptive clustering algorithm when the K^t is under 40. It stabilizes
 398 the RMSE between 0.08 (weekdays) and 0.06 (weekends) when benchmarks
 399 have a tendency to fluctuate. After removing the 30 first days of convergence
 400 to a stable solution, the overall RMSE score of the online adaptive clustering
 401 algorithm is 7.2% against 7.5% and 7.9% respectively for the K-means and
 402 SOM. In terms of computational time, on a desktop computer equipped with
 403 Intel Xeon CPU 3.50 GHz \times 8 cores, the consensus clustering (computed

404 in parallel on 7 cores) takes 15 minutes to be completed, and each iteration
405 of the online adaptive clustering (on a single core) takes approximately 1
406 minute 20 seconds as the overall process on 240 days took 6 hours. As com-
407 parison, the SOM takes 16 hours to be completed and the K-means 20 hours.
408 These results confirm the necessity of having an adaptive clustering process
409 that estimates correctly the number of clusters in the data at time t . The
410 difference of performance between the online adaptive clustering algorithm
411 and the benchmark would be larger with a dataset displaying more non-
412 stationary behavior like loads involved in Demand Response (DR) programs
413 or with large amount of PVs.

414 Figure 8 gives an example of the evolution of a cluster over the period.
415 The shape of the typical load profile as well as the lowest value are changing
416 over the period. The cluster groups mostly restaurants, which are active
417 daily from lunch to dinner time with a peak at dinner time and along the
418 year at high activity periods (Christmas holidays, Saturdays, and from April
419 to August).

420 From the application on real data the algorithm has fulfilled expectations,
421 it handles correctly slow changing and fast changing profiles, splitting and
422 merging to keep the same overall accuracy with a low computational cost at
423 every iteration.

424 6. Conclusions and Future Works

425 In this paper, we have presented an online adaptive clustering methodol-
426 ogy for load profiling. We have demonstrated its efficiency on both synthetic
427 and real datasets. It is more agile than traditional clustering based load

428 profiling as it is recursive and uses the most recent data to update daily
429 typical load profiles and computationally **efficient** as it processes only short
430 time series at each time step of the online clustering. In this framework, the
431 typical load profiles are generated every day, hence a customer's profile can
432 be summarized by concatenating the typical load profiles assigned for each
433 day to generate its load profile over a period of interest.

434 The methodology establishes a first step toward dynamic profiling of elec-
435 tricity consumption patterns. The deployment of smart meters associated
436 with the increasing share of renewables will make dynamic load profiling
437 compulsory for future grid management as fast decision making under uncer-
438 tainty is becoming the common situation. A dynamic clustering methodology
439 is then more suited for handling balancing between generation and consump-
440 tion which is a dynamic problem both on production and demand sides.

441 From a widespread power system perspective, the methodology can be a
442 systematic tool providing insights at a reasonable time scale for demand side
443 management programs. It can also be used to develop new dynamic tariffs
444 that would reflect the marginal cost each customer generates by shifting or
445 synchronizing their peak load to the overall peak load. In electricity demand
446 analysis a dynamic load profiling method will provide information on the
447 stability of customers load patterns over time and whether it displays some
448 periodicity (e.g. day open and close for a supermarket). Classic load profiling
449 applications like estimating load for planning of the grid will also benefit from
450 the output of the online adaptive clustering algorithm. Sampling of the most
451 probable weekly or yearly load profiles can be generated by concatenating the
452 daily load profiles and provides information on the uncertainty of the load

453 behavior *via* confidence intervals or probability density distribution around
454 the curve.

455 Several possible extensions of the work can be considered; the method-
456 ology could be extended to multi-energy profiling which is lacking at the
457 moment and will be needed as multi-energy solutions exploiting volatility of
458 different markets are being deployed (e.g. fuel shifting solution). **It could**
459 **also be tested on a dataset with large amounts of non-stationary loads, typ-**
460 **ically households subject to DR or equipped with PVs, EVs and batteries.**
461 **As the code has been made available on *GitHub*², we invite readers with such**
462 **dataset to download the code and test it on their data.** On a more techni-
463 cal aspect, the methodology could be transposed in a Bayesian framework,
464 which will provide direct evaluation of the uncertainty.

465 **Acknowledgment**

466 The authors thank EnergyLab Nordhavn partners, Radius and HOFOR
467 for supporting this work by providing data, as well as the EUDP for funding
468 through the EnergyLab Nordhavn project (EUDP 64015-0055).

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