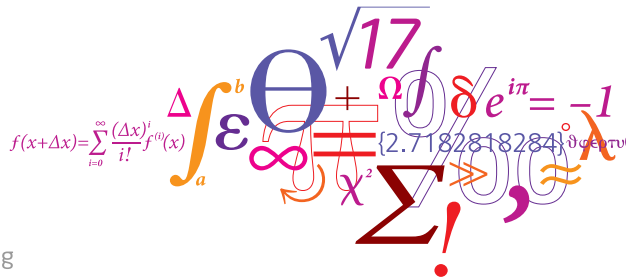


## Market power in electricity markets

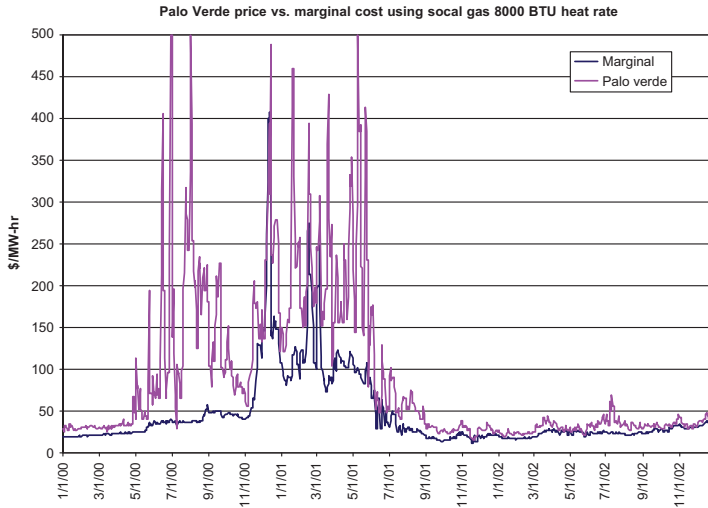
Strategic behavior, free-riders, spiteful bidders, ...

Vladimir Dvorkin

Technical University of Denmark (DTU)



# California energy crisis



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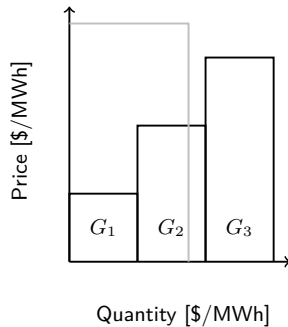
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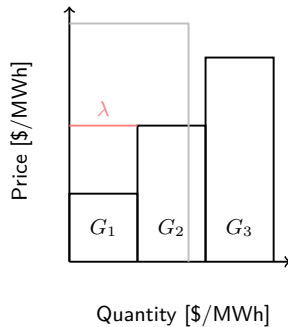
## Outline

- Illustrative example
- Modeling market power
- Numerical experiments
- References

# Let's make a thought experiment

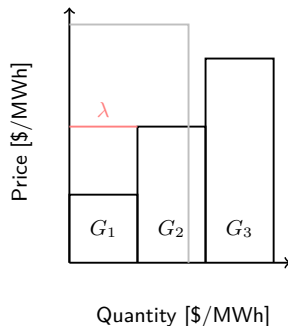


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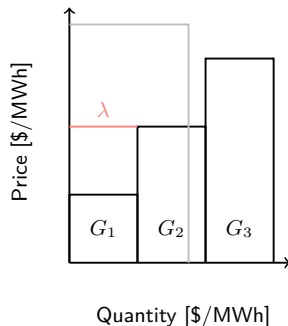
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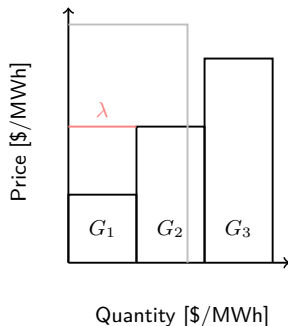


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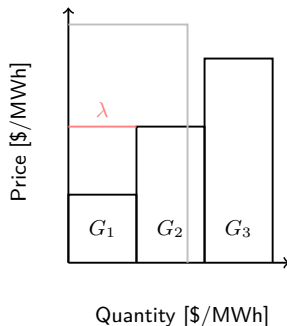
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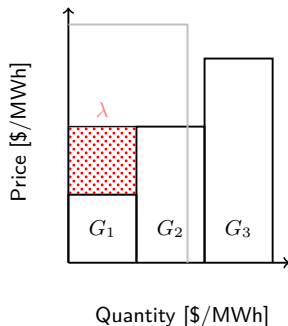
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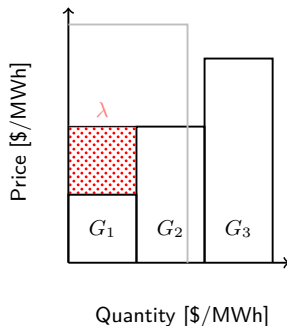
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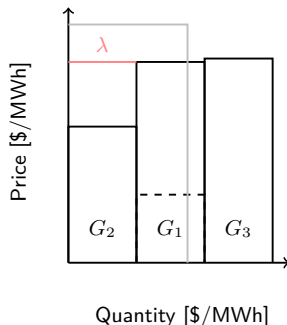
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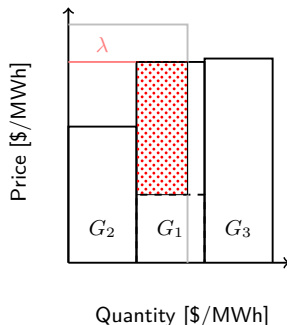
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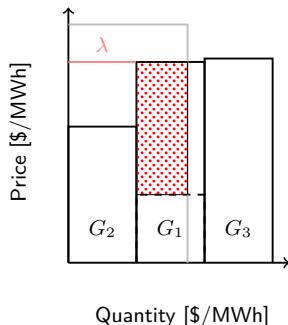
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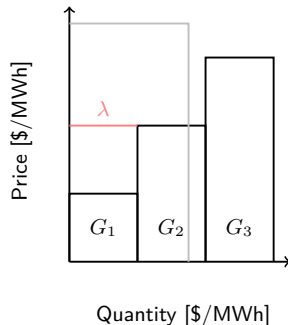
Some observations:

- By bidding **strategically**,  $G_1$  can significantly increase its profit
- Unit  $G_2$  is a **free-rider**
- Operating cost can be **drastically** increased!



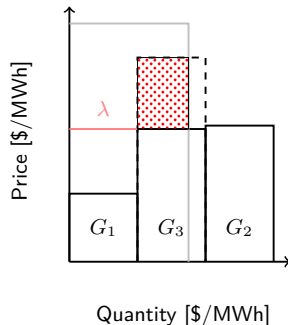
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What about  $G_3$  that is currently out of market? Can you do something to make it profitable?



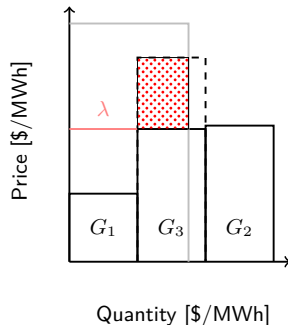
## Let's make a thought experiment

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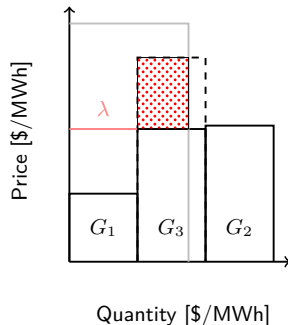
## Illustrative example

## Let's make a thought experiment

- What about  $G_3$  that is currently out of market? Can you do something to make it profitable?
- Sure you can! But it will take some time
- What is your objective function in this case?

$$(\lambda - c_2)p_2 \leftarrow \min$$

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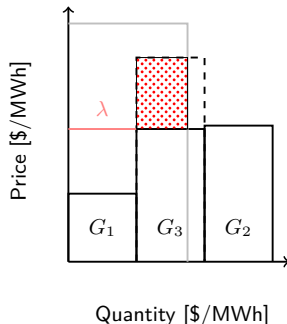


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Some observations:

- Market power is not only about profit maximization. It could be exercised to damage others' standing
- Indeed,  $G_3$  is a **spiteful bidder!**
- $G_3$  is interested in the short-term loss-making strategy to gain more significant long-term benefits

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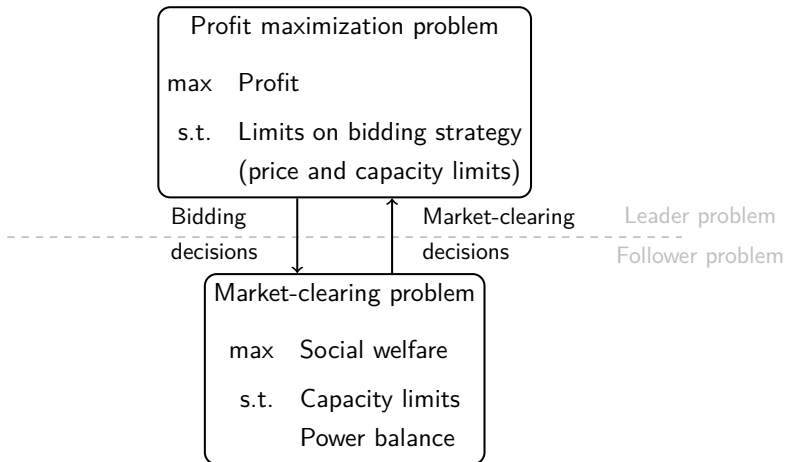
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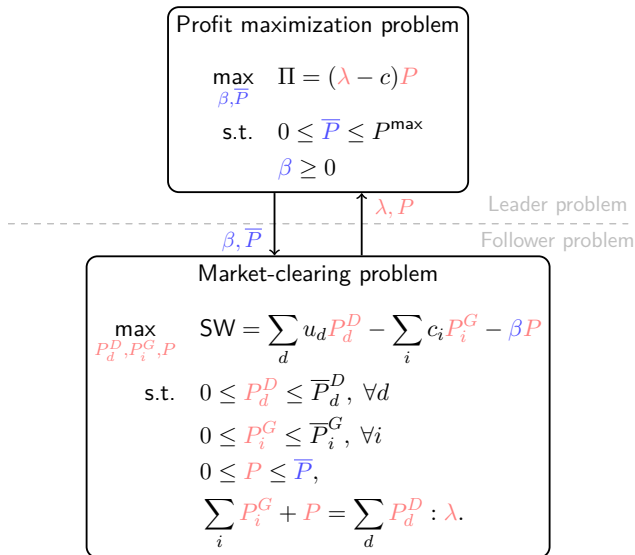
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- 👉 We will solely focus on *Stackelberg game*



# Modeling market power

## Stackelberg game

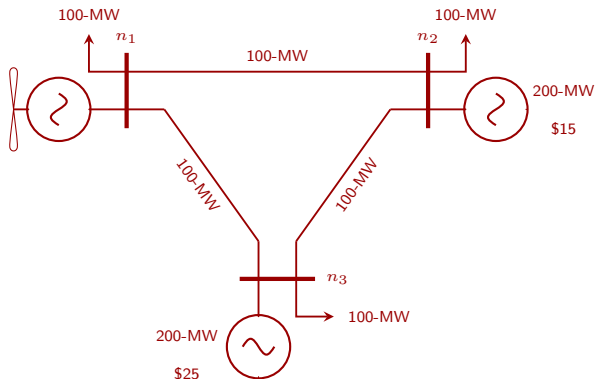




## Numerical experiments

# Test case description

- Three-node system with one wind and two conventional units
- Loads are inelastic, and the price-cap is set to 200\$/MWh
- We are aiming at studying the market power of unit  $G_2$



## Let's study the market power of the unit at node two

- 👉 We will study the market outcomes under different wind penetration levels
- 👉 Three cases:
  - $G_2$  - **non-strategic**, i.e. it enters the market with **actual** production cost. This corresponds to the *perfect competition*

$$\begin{aligned} \max \quad & (\lambda - c_2)p_2 \\ \text{s.t.} \quad & \beta = c_2 \end{aligned}$$

where  $\lambda$  - price,  $c_2$  - cost,  $p_2$  - scheduled quantity,  $\beta$  - price bid

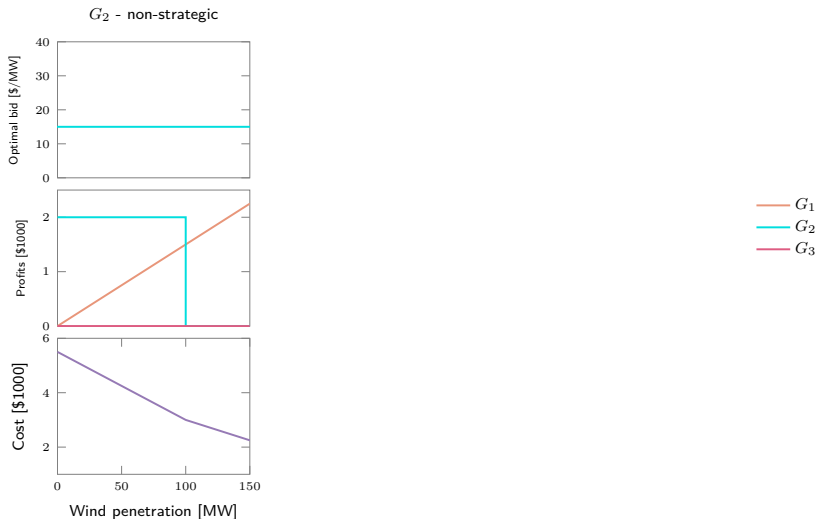
- $G_2$  - **strategic and profit-maximizer**. It aims at finding such price bid that maximizes its profit

$$\begin{aligned} \max \quad & (\lambda - c_2)p_2 \\ \text{s.t.} \quad & \beta \geq 0 \end{aligned}$$

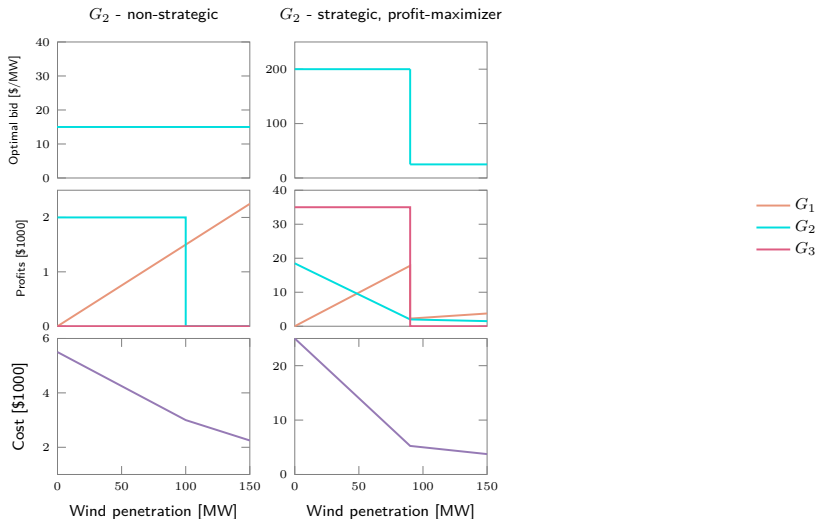
- $G_2$  - **strategic and spiteful**. It aims at finding such price bid that minimizes rivals' profits

$$\begin{aligned} \min \quad & (\lambda - c_1)p_1 + (\lambda - c_3)p_3 \\ \text{s.t.} \quad & \beta \geq 0 \end{aligned}$$

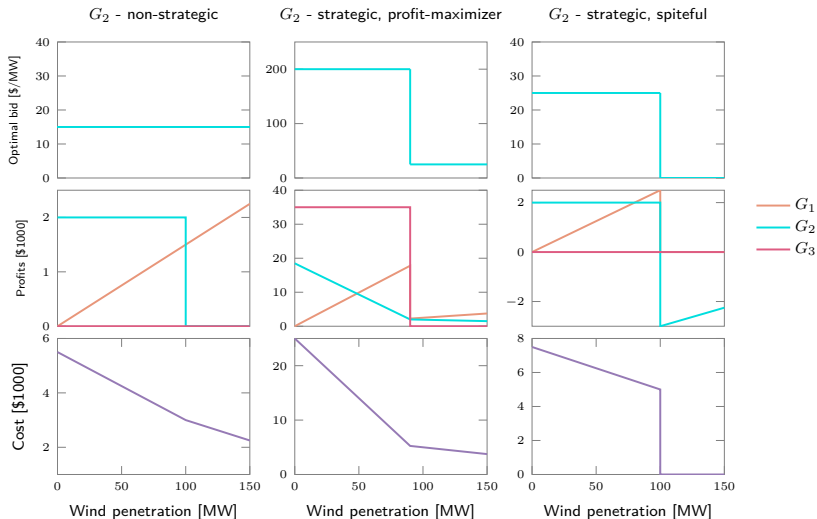
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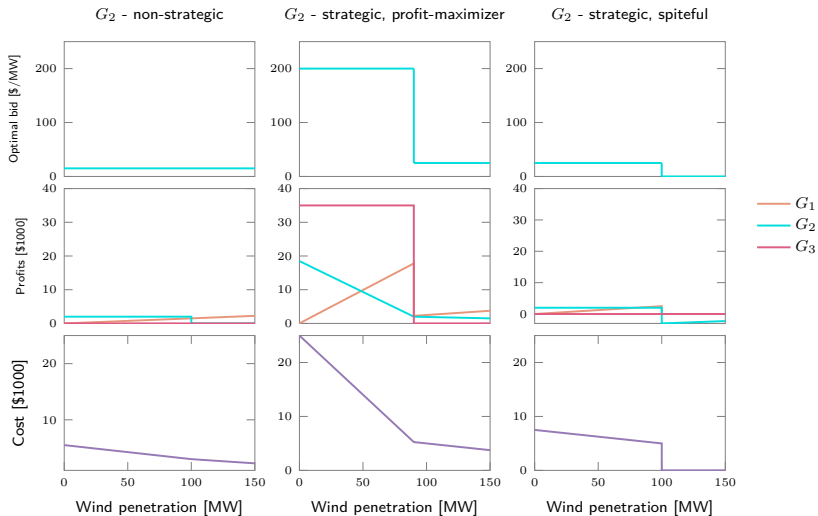
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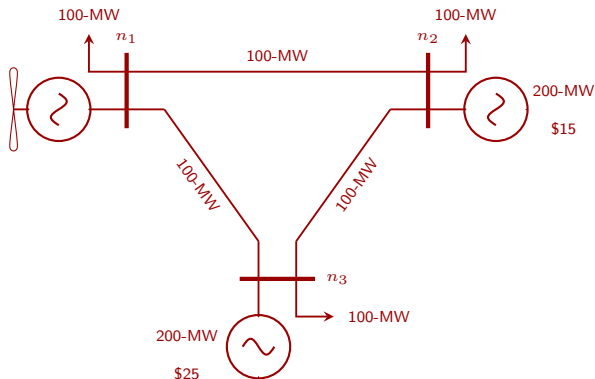




## Numerical experiments

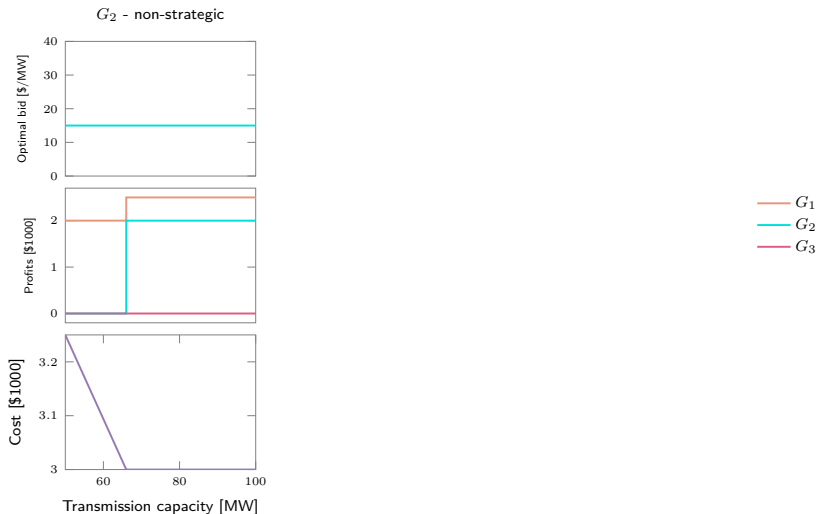
# Impact of network congestion

- Let's fix wind power capacity to 100 MW
- By varying transmission capacity of lines 1-2 and 3-2, we will see how strategy of unit  $G_2$  and market outcomes change



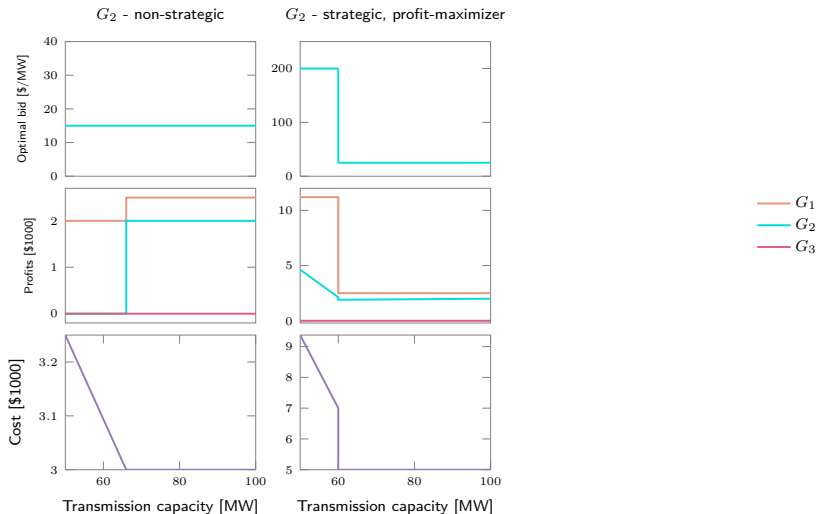
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## Impact of network congestion



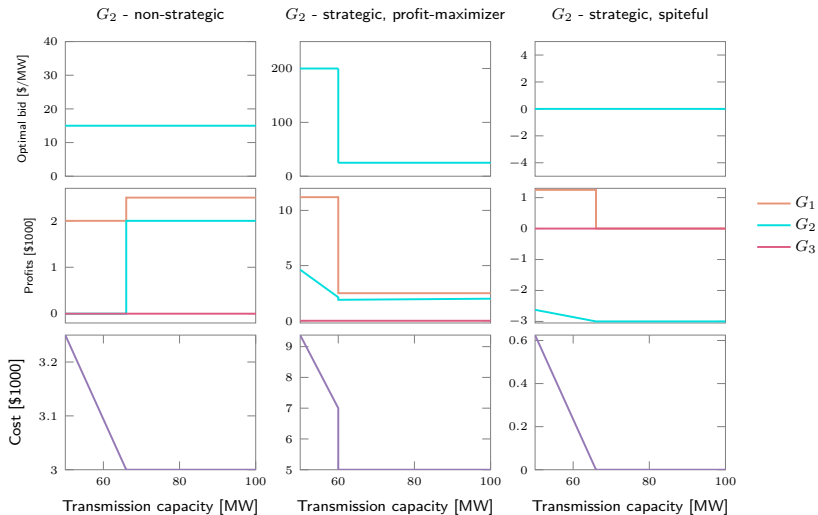
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## Main findings

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- 👉 From Enron's audiotapes
  - *What's happening?*
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  - *Burn, baby, burn! That's a beautiful thing.*
- 👉 By modeling the strategic behavior of generation companies, regulators can identify the ways to reduce their market power and enhance the efficiency of the existing design.

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- 👉 And many other options (check references)

Thank you for your attention!

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